Fluorescence quenching of 5-methyl-2-phenylindole (MPI) by carbon tetrachloride in different solvents and temperatures

Kalpana M Painagoni¹, H D Patil²

¹Department of Physics, Government First Grade College, Gokak, Karntaka, India ²Department of Physics, Basaveshwar Science College, Bagalkot, Karntaka, India

Abstract: The fluorescence quenching of 5-methyl-2-phenylindole (MPI) by carbon tetrachloride by steady state in different solvents, and by transient method in benzene has been carried out at room temperature. The Stern–Volmer (SV) plot has been found to be non-linear with a positive deviation for all the solvents studied. In order to interpret these results we have invoked the ground state complex and sphere of action static quenching models. Using these models various rate parameters have been determined. The magnitudes of these parameters imply that sphere of action static quenching model agrees well with the experimental results. Hence the positive deviation in the SV plots is attributed to the static and dynamic quenching. Further, from the studies of temperature dependence of rate parameters and lifetime measurements, it could be explained that the positive deviation is due to the presence of a small static quenching component in the overall dynamic quenching. With the use of finite sink approximation model, it was possible to check whether these bimolecular reactions as diffusion limited and to estimate independently distance parameter R' and mutual diffusion coefficient D. Finally an effort has been made to correlate the values of R' and D with the values of the encounter distance R and the mutual diffusion coefficient D determined using the Edward's empirical relation and Stokes–Einstein relation.

Keywords: Fluorescence quenching; MPI; Solvent effect; Finite sink approximation model; Sphere of action static quenching model

I.

Introduction

Fluorescence quenching of aromatic hydrocarbons in solvents by various quenchers like aniline, bromobenzene, carbon tetra chloride (CCl₄), ethyltrithiocarbonate, halide ions, metal ions, etc. has been a subject of continued investigation for the last couple of decades [1-11]. The study has been mainly to understand the nature of biomolecular reactions taking place both under study state and transient conditions. This study has not only been of importance in physical sciences but also in chemical, biological and medical sciences[12-18]. The fluorescence yield in bimolecular liquid systems is hindered due to several mechanisms such as static and dynamic quenching, excimer and exciplex formation, charge transfer processes, etc. One of the well-known experimental techniques used to study the role of fluorescence quenching is to determine the quenching rate parameter using Stern–Volmer (SV) plots. If the quenching mechanism is mainly due to dynamic process, then it will be largely due to diffusion in which case diffusion rate parameter k_d equals the quenching rate parameter kq (= K_{sv}/τ_0) where K_{sv} is the slope of the linear plot and t0 is the decay time of the solute in the absence of the quencher. On the other hand, if the experimental results do not simulate with the simple linear SV equation, then it may be due to one of the above processes other than or along with diffusion processes. In the present study we have used both steady-state and transient experimental setup to investigate the quenching of 5-methyl-2-phenylindole (MPI)by CCl₄ in four different organic solvents with a view to understand the nature of quenching mechanism involved in these systems. MPI is widely used as a Laser dye and has several applications such as anticoagulants fluorescence indicator and optical brightness properties [14]. The various rate parameters responsible for fluorescence quenching have been determined by sphere of action static quenching model. In the light of these rate parameters, lifetime measurements and dependence of quenching rate parameter on the temperature of the medium, the possible quenching mechanisms are discussed.

II. Theory

The dynamic process in which quenching mechanism is mainly due to collision is governed by the linear SV equation

$$I_{o}/I = 1 + K_{sv}[Q],$$
(1)
$$\tau_{o}/\tau = 1 + K'_{sv}[Q],$$
(2)

where I_o and τ_o are the fluorescence intensity and fluorescence lifetime in the absence of quencher, I and τ are the fluorescence intensity and fluorescence lifetime in the presence of quencher [Q], K_{sv} (= $k_q \tau_o$) and K_{sv} (= $k_q^2 \tau_o$)

 τ_{o}) are SV constant and k_{q} (= k_{q} ') is the quenching rate parameter. Eqs. (1) and (2) are applicable as long as the experimental results show linear variation. The departure from linearity in SV plot, suggests that quenching mechanism is not purely collisional and this may be attributed either to the ground state complex formation or to the sphere of action static quenching model [7].

In order to see whether the ground state complex formation is partly playing a role, one can use extended SV equation [19, 20] given by

$$[(I_o/I) - 1]/[Q] = (K_{sv} + k_g) + (K_{sv}k_g) [Q]$$
(3)

where K_{sv} is the SV constant and k_g is the ground state association constant. From Eq. (3), the values of K_{sv} and k_g can easily be determined by least-squares fit method.

The ground state complex formation takes place if quenching constant $k_q (= K_{sv}/\tau_o)$ obtained from Eq. (3) agrees well with that obtained from the lower portions of the plot according to Eq. (1). In that case static quenching is very low. Apart from this, the ground state complex formation may be noticed if there is a change in the absorption and fluorescence spectra even at higher concentrations of quencher.

In order to see whether static quenching process is playing a role, one can use "sphere of action static quenching model". According to this model, the instantaneous or static quenching occurs if the quencher molecule is very near to, or in contact with the fluorescent molecule at the exact moment it happens to be excited. This was explained by the fact that only a certain fraction 'W' of the excited state is actually quenched by the collisional mechanism. Some molecules in the excited state, the fraction of which is (1-W), are deactivated almost instantaneously after being formed, because a quencher molecule happens to be randomly positioned in the proximity at the time the molecules are excited and interacts very strongly with them. Several models were employed (Smoluchowski model) [21, 22] to describe this static quenching process, all leading to the following modified form of the SV equation.

$$(I_o/I) = 1 + K_{sv}[Q]/W$$
 (4)

As W depends on the quencher concentration [Q], the SV plots for a quencher with a high quenching ability generally deviate from linearity. Thus it is worth rewriting Eq. (4) as

 $[1-(I_o/I)]/[Q] = (K_{sv}(I_o/I) + (1-W)/[Q]$ (5) From Eq. (5) one can easily calculate K_{sv} and the values of W by least-squares fit method. According to Zeng et al. [20] and Andre et al. [24], if the distance between the quencher molecule and the excited molecule lies between the encounter distance and the kinetic distance, the static effect takes place especially in the case of steady-state experiments irrespective of ground state complex formation provided reactions are limited by diffusion.

III. Experimental details

he solute MPI was a generous gift from a colleague from Department of Chemistry, Gulbarga University, Gulbarga and is of scintillation grade. The molecular structure of MPI is shown in Fig. 1. The quencher CCl₄ was obtained from BDH laboratory, UK and was of HPLC grade. All other solvents were obtained from s-d fine chemicals Ltd., India. They were of spectroscopic grade and used without any further purification. The solutions were prepared keeping the concentration of MPI fixed $(1X10^{-4} \text{ M})$ and varying the quencher concentration (0.02–0.10 M) in all the solvents. Fluorescence spectrophotometer F-2000 (Hitachi Japan make Bandwidth 10 nm) was used for fluorescence intensity measurements, with perpendicular geometry. Fluorescence measurements were made taking fresh solution each time in a rectangular quartz cell having an airtight stopper. The solute has maximum absorption at 280 nm. The solute was excited at 280 nm and the fluorescence spectrum was recorded. The maximum fluorescence corresponds to 332 nm. First the fluorescence intensity I_0 was measured without the quencher and then the fluorescence intensity I was measured at different quencher concentrations and at a fixed solute concentration. Measurement of fluorescence lifetime of the solute with and without quencher, and at different temperatures was made by single photon counting time-domain spectrometer (Edinburgh Instrument, UK, Model EI-199). Hydrogen gas was used to fill the Lamp of the single photon counting (SPC) system at 0.6 atm pressure, keeping electrode separation 0.7 mm, applying the discharge voltage of about 7 kV and operating the Lamp at a frequency of 30 kHz, with this setting, Lamp pulses having pulse width of about 1 ns at FWHM were obtained. A nonlinear least-squares iterative reconvolution mathematical procedure was used here. The fluorescence lifetime data were analyzed by considering reduced chi-square (χ_r^2) value. The observed fluorescence decays were monoexponential. It has been found that the value of (χ_r^2) is nearly equal to 1. The experimental values are reproducible within 5% of the experimental error. Description of the experimental setup is discussed elsewhere [13].

3. Tables and Figures

3.1. Tables

Table 1.The values of Stern–Volmer constant K_{sv}, bimolecular quenching rate parameter k_q, static quenching constant V and kinetic distance r for different solvents.

Solvent	Ksv (M ⁻¹)	k _q X10X ⁻¹⁰ (M ⁻¹ s ⁻¹)	V (mol ⁻¹ dm ³)	r(Å)
Toluene	78.78	10.00	22.34	20.69
Benzene	19.51	2.49	2.73	9.80
Cyclohexane	22.80	2.91	58.09	28.40
DMSO	15.90	2.03	14.78	18.00
$R_{Y} = 3.98 \text{ Å}$, $R_{Q} = 2.73 \text{ Å}$, $\tau_{o} = 0.784 \text{ ns}$.				

Table 2. The values of K_{sv}^0 (steady-state quenching constant at [Q] = 0), mutual diffusion coefficient D, distance parameter R', $4\pi N'DR'$, quenching rate parameter k_q , coefficient of viscosity η and solvent polarity ε

Solvent	$\frac{K^0_{sv}}{(\mathrm{dm^3\ mol^{-1}})}$	D x 10 ⁵ (cm ² s ⁻¹)	R' (Å)	$4\pi N' DR' x 10^{-10}$ (M ⁻¹ s ⁻¹)	kq x10 ⁻¹⁰ (M ⁻¹ s ⁻¹)	η(m pasec)	3
Toluene	53.10	7.50	11.93	6.77	10	0.59	2.38
Benzene	0.146	36.60	0.68	0.012	2.49	0.65	2.28
Cyclohexane	19.35	2.50	13.04	2.47	2.91	0.98	2.02
DMSO	8.32	2.19	6.40	1.06	2.03	2.20	4.70

$$R (= R_Y + R_Q) = 6.71 \text{ Å}.$$

Table 3. The values of mutual diffusion coefficients D^a and D^b, distance parameter R` and encounter distance R

Solvent	$D^{a} \times 10^{5} (cm^{2}s^{-1})$	$D^{b} \times 10^{5} (cm^{2}s^{-1})$	R` Å
Toluene	3.91	7.50	11.93
Benzene	2.39	36.60	0.675
Cyclohexane	2.20	2.50	13.04
DMSO	0.98	2.19	6.40

$$R (= R_Y + R_Q) = 6.71 \text{ Å}.$$

^aDiffusion coefficients determined from Stoke–Einstein relation.

^bDiffusion coefficients determined from finite sink approximation model.

 Table 4. The values of intercept, range of W, static quenching constant V and radii of the sphere of action (kinetic distance) r for (MPI+CCl₄) system at different temperatures

action (Kincuc ui	stance i for (mit r co	14) system at uniteren	i icinperatures	
Temperature (°C)	Intercept	Range of W	V(mol ⁻¹ dm ³)	r (Å)
30	4.44	0.56-0.91	5.86	13.2
40	6.66	0.33-0.87	10.90	16.2
50	1.89	0.81-0.96	2.09	9.39
60	3.79	0.62-0.92	4.76	12.3

$$R_Y$$
 (MPI) = 3.98 Å, R_Q (CCl₄) = 2.73 Å, $R (= R_Y + R_Q) = 6.71$ Å.

Table 5. The Stern–Volmer quenching constant K_{sv} , the quenching rate parameter k_q at different temperatures and the activation energy E_q for collisional quenching process for (MPI+CCl₄) system

system.				
Temperature (°C)	$K_{sv}(M^{-1})$	$k_q x 10^{-9} (M^{-1} s^{-1})$	E _q (kJ mol ⁻¹)	
30	5.57	6.61	20.29	
40	6.66	7.90		
50	9.73	11.54		
60	11.12	13.19		

3.2 Figures



Fig. 1. Molecular structure of MPI



Fig. 2. Stern-Volmer plots of I/Io against [Q] in different solvents.



Fig. 3 Absorption spectra of MPI (C=1x10⁻⁴M) in the presence of CCl₄ in hexane at 27°C. Concentrations of CCl₄ (0.00, 0.02, 0.04, 0.06, 0.08 and to 0.10 M)



Fig. 4. Fluorescence emission spectra of MPI (C = 1 x 10^{-4} M, λ_{ex} = 280 nm) in presence of CCl₄ in benzene at 27°C. Concentrations of CCl₄ (0.00, 0.02, 0.04, 0.06, 0.08 and to 0.10 M)



Fig. 5. Plots of [1-(I/I₀)]/[Q] against I/I₀ for MPI + CCl₄ system in different solvents.



Fig. 6. Plots of K⁻¹_{sv} versus [Q]^{1/3} in different solvents.



system in benzene at different temperatures.



Fig 8. Plot of $\ln k_q$ versus $10^3/T$ for MPI + CCl₄ system.



Fig. 9 Fluorescence decay profiles of MPI at different quencher concentrations of CCl₄ (0.00, 0.02, 0.04, 0.06, 0.08 and 0.10 M).



Fig. 10. Stern-Volmer plot of τ_0/τ versus [Q] in benzene for MPI + CCl₄ system

IV. Results and discussion

The SV plots obtained by using the experimentally determined values of I_0 and I are found to be nonlinear in all the solvents showing positive deviation and are shown in Fig. 2. Similar experimental results were also observed by others [1–6]. Thus, positive deviation from linearity suggests that quenching is not purely collisional and this may be attributed either to the ground state complex formation or to the sphere of action static quenching model [7].

The values of K_{sv} from Eq. (3) were found to be imaginary in all the solvents. Therefore, the role of ground state complex formation is ruled out in the present case. This is also confirmed by the fact that there is no shift in the peak position in the absorption spectrum of MPI in hexane, and emission spectrum of MPI in benzene at different quencher concentrations as shown in Figs. 3 and 4. These facts show that Eq. (3) is not applicable for the analysis of the data corresponding to the observed positive deviation in the SV plots. Thus the analysis of the data for positive deviation in the SV plot was made using "sphere of action static quenching model". Fig. 5 shows the plots of [1-(I/I_o)]/[Q] against I/I_o for MPI with CCl₄ as quencher in different solvents which are linear according to Eq. (5).

The dynamic quenching constant K_{sv} is determined in all the cases by least-squares fit method using Eq. (5) and the values are given in Table 1. Fluorescence lifetime τ_0 is given at the bottom of Table 1. Bimolecular quenching rate parameter k_a was determined from the experimentally determined values of K_{sv} and τ_o according to the relation $k_{\rm q} = K_{\rm sv}/\tau_{\rm o}$ and the values are given in Table 1. In order to support static and dynamic effects, we have determined the magnitudes of static quenching constant V and radii r of sphere of action (or kinetic distance) using the abovementioned theory for sphere of action model. By using equations $W = e^{-V[Q]}$, $V/N_0 =$ $(4\pi r^3)/3$ and (5) the values of V and r are determined by least-squares fit method in all the solvents and are given in Table 1. Similar results were also obtained by others [7, 12, 29]. The radii of the solute (R_Y) and the quencher (R₀) molecules were determined by adding the atomic volumes of all the atoms constituting the molecule as suggested by Edward [23] and are given at the bottom of Table 1. From these values of $R_{\rm Y}$ and $R_{\rm O}$, the sum of the molecular radii [R] of the solute MPI and the quencher CCl₄ is determined. This sum of the molecular radii R is referred to as encounter distance or contact distance or reactive distance. This value of R is then compared with the values of 'r' to verify whether the reaction is due to sphere of action model. From Table 1 we see that the values of kinetic distance 'r' are greater than the encounter distance R. Therefore, according to Zeng et al. [20] and Andre et al. [24] the static effect takes place irrespective of ground state complex formation provided reactions are limited by diffusion indicating that the sphere of action model holds well in our case also. Further it may also be noted that a positive deviation in SV plot is expected when both static and dynamic quenching occurs simultaneously [19].

Further to find out whether the reactions are diffusion limited we invoke the finite sink approximation model [25–27] for steady state which helps us to estimate independently the mutual diffusion coefficient D, distance parameter R' and activation energy-controlled rate constant k_a . The modified SV equation [20].

$$k_{sv}^{-1} = \left(k_{sv}^{0}\right)^{-1} - \frac{\left(2\pi N'\right)^{1/3}}{4\pi N' D\tau_{0}} [Q]^{1/3}$$

$$K_{sv}^{0} = \frac{4\pi N' DR\tau_{o}k_{a}}{4\pi N' DR + k_{s}}$$
(6)
(7)

Finite sink approximation model is used to determine the values of D, R_o and k_a. For efficient quenching processes the value of K_{sv} is often observed to increase with [Q] [20]. Hence the values of K_{sv} were determined at each quencher concentration in all the solvents and the values of k_{sv}^{-1} are also determined. Fig. 6 shows the plots of k_{sv}^{-1} against [Q]^{1/3}. From these figures we see that all the plots in different solvents are almost linear and small deviation may be due to experimental uncertainties. Hence, the linear dependence of k_{sv}^{-1} on the one-third power of quencher concentration within the error limits is confirmed [20]. Then the least-squares fit value of K_{sv}^{0} (SV constant at [Q] = 0) was obtained from the intercept of the plot of k_{sv}^{-1} against [Q]^{1/3}, according to Eq. (6). Similarly, mutual diffusion coefficients D were determined from the slope of the Eq. (6) by least-squares fit method and the values of K_{sv}^{0} and D are given in Table 2. Using these values of K_{sv}^{0} and D, the distance parameter R_o was determined according to equation K_{sv} = $4\pi N' DR' \tau_o$ and the values are given in Table 2. According to Joshi et al. [28] the bimolecular reactions are said to be diffusion limited if the values of k_q (determined from Eq. (5)) are greater than $4\pi N' DR'$. Hence the values of $4\pi N' DR'$ are calculated using the experimentally determined values of R_o and D of Eq. (6) and are given in Table 2. We see from the table that

in all the solvents the values of k_q are greater than $4\pi N'DR'$, which is an expected result for diffusion-limited reaction [27]. When we compare the quenching rate parameter k_q with solvent polarity and viscosity, it is found that k_q is independent of solvent polarity but depends on solvent viscosity. This fact is clear from Table 2. While k_q is high in toluene, the less viscous solvent, it is low in DMSO, the most viscous solvent. Hence no correlation exists between k_q and solvent polarity.

It is important to note that, when an attempt was made to correlate the experimentally determined values of mutual diffusion coefficient D and distance parameter R' using finite sink approximation model with the corresponding values of D and R calculated from Stoke-Einstein relation and Edward's empirical relations respectively in all the systems, the values of D and R' (or R) determined from the two methods are quite comparable. From Table 3 it is clear that correlation fails in some other solvents. Similar discrepancies have also been observed by others [20, 28] in some bimolecular quenching reactions. This may be due to the uncertainties in the values of adjustable parameter 'a' in the Stoke's-Einstein relation and the approximation in the values of atomic volume in the Edward's relation. Hence we may conclude that finite sink approximation model is valid in recovering the parameters D and R'(or R). In order to check whether these reactions are diffusion limited, the temperature dependence of rate constant k_q is examined. The fluorescence quenching was carried out in the temperature range 30–60° C by both steady state and transient methods. Fluorescence lifetime τ_o of MPI at different temperatures is measured by single photon counting time-domain spectrometer (Edinburgh Instrument, UK, Model EI-199). No variation in fluorescence lifetime with temperature was observed. This may be due to the following fact. The molecular structure of MPI may be such that the gap between S1 and T2 may be narrow or may lie on the same line or such that even state order gets inverted on heating, i.e. T2 lies below S1. When this happens, there is no increase in the rate of non-radiative intersystem crossing. Hence the lifetime of MPI remain almost constant over the temperature range of our study [30]. Therefore, we have used the average value of τ_{av} (= 0.844 ns) at all temperatures. The SV plots at all temperatures show positive deviation. By using Eq. (5), the plot of [1-(I/I_o)]/[Q] against I/I_o was plotted at all temperatures and shown in Fig. 7. From linear fit values, K_{sv} and V are determined and are listed in Table 4. The values of quenching rate k_q was calculated at all temperatures and listed in Table 5. From this table it is clear that K_{sv} increases with temperature since k_{diff} increases, as expected. K_{sv} depends on temperature through the temperature dependence of rate constant k_{q} and the fluorescence lifetime $\tau(t)$. It has been assumed that k_q is proportional to exp (-Eq/RT) [1]. Where E_q is the activation energy for collisional process, R the gas constant and T the absolute temperature. Thus the value of E_{g} can be determined on the slope of the plot lnkq versus inverse of the absolute temperature T. Fig. 8 shows the plot of lnkq versus 10^3 /T for MPI+CCl₄ system. From this figure it can be seen that the plot is linear. From the least-squares fit value of the slope of this plot, the value of E_q has been determined and is given in Table 5. Similar values of E_q have been obtained by others also [1–4]. The values of E_q being approximately equal to the values obtained by others suggest that the rates of reactions are limited by diffusion of the reactants through the solvents. These facts suggest the presence of static quenching component in overall dynamic quenching. The fluorescence decay profile for MPI+CCl₄ in benzene at different quencher concentrations is shown in Fig. 9. Further, we checked whether a transient effect also play a role in the overall dynamic quenching process. If transient effect is playing a role, the plot of (τ_0/τ) against [Q] is not linear. But from Fig. 10, it is observed that the plot of (τ_0/τ) against [Q] is linear. It indicates that transient effect is not playing a role in quenching process. This fact is also supported by the variation of static quenching constant with temperature. Thus the linearity of (τ_0/τ) with [Q] and the variation of V prompt us to suggest that positive deviation in the SV plot in the system is due to the presence of static quenching component in overall dynamic quenching.

V. Conclusion

From the above discussion we observe that: (1) the SV plots show positive deviation leading to high values of k_q , indicating efficient fluorescence quenching. (2) Static quenching constant 'V' and kinetic distance 'r' are in agreement with the corresponding literature values. (3) The value of k_q is greater than $4\pi N'DR'$ in all solvents. (4) Further, the values of R' and D determined from the finite sink approximation model are close to the values determined from Edward's and Stokes–Einstein empirical relations, respectively. In view of the above facts we may conclude that quenching reaction is diffusion limited and both static and dynamic quenching processes are partly playing a role in this system.

References

- [1] R. Roy, S. Mukherjee, Chem. Phys. Lett. 140 (1987) 210.
- [2] J. Tipperudrappa, D.S. Biradar, M.T. Lagare, S.M. Hangodimath, S.R. Inamdar, J.S. Kadadevarmath, J. Photochem. Photobiol. A: Chem. 177 (2006) 89.
- [3] D. Goswami, R.S. Sarpal, S.K. Dogra, Bull. Chem. Soc. Japan 64 (1991) 3137.
- [4] S.M. Hangodimath, G.S. Gadginmath, G.C. Chikkur, Appl. Radiat. Isot. 41 (1990) 817.
- [5] A. Rani, S.J. Sobhanadri, T.A. Prasad Rao, J. Photochem. Photobiol. 33 (1996) 749.
- [6] P.K. Behra, T. Mukhergee, A.K. Mishra, J. Lumin. 65 (1995) 131.

- [8] M. Swaminathan, N. Radha, Spectrochim. Acta Part A 60 (2004) 1839.
- [9] C. Hariharan, A.K. Mishra, Radiat. Meas. 32 (2) (2000) 113.
- [10] H.M. Suresh Kumar, R.S. Kunabenchi, J.S. Biradar, N.N. Math, J.S. Kadadevaramath, S.R. Inamdar, J. Lumin. 116 (2006) 35.
- [11] S. Nigam, S.K. Dogra, Ind. J. Chem. 32A (1993) 290.
- [12] S.M. Hanagodimath, G.C. Chikkur, G.S. Gadaginmath, Chem. Phys. 148 (2,3) (1990) 347.
- [13] J.S. Kadadevaramath, T.P. Giraddi, G.C. Chikkur, Radiat. Meas. (USA) 26 (1) (1996) 17.
- [14] P. Cyril, S.A. Maged, J.J. Aaron, B. Michada, T. Alphonse, C. Lamine, Spectrosc. Lett. 27 (4) (1994) 439.
- [15] S.M. Hanagodimath, G.C. Chikkur, G.S. Gadaginmath, Acta Phys. Pol. A 81 (3) (1992) 361.
- [16] S.M. Hanagodimath, G.C. Chikkur, G.S. Gadaginmath, Pramana J. Phys. (India) 37 (2) (1991) 153.
- [17] E.A. Lissi, M.V. Encians, S.G. Birtolotti, J.J. Cosa, C.M. Previtali, Photochem. Photobiol. 51 (1990) 53.
- [18] S. Nigam, M. Belletete, R.S. Sarpal, G. Durocher, J. Chem. Soc. Faraday Trans. 91 (1995) 2133.
- [19] P.K. Behera, A.K. Mishra, J. Photochem. Photobiol. A: Chem. 71 (1993) 115.
- [20] H. Zeng, G. Durocher, J. Lumin. 63 (1995) 75.
- [21] J.M. Frank, S.J. Wawilow, Z. Phys. 69 (1931) 100.
- [22] A.Y. Moon, D.C. Poland, H.A. Scheraga, J. Phys. Chem. 69 (1965) 2960.
- [23] J.T. Edward, Chem. Ind. (London) (1956) 774.
- [24] J.C. Andre, M. Niclause, W.R. Ware, Chem. Phys. 28 (1978) 371.
- [25] J. Keizer, J. Phy. Chem. 86 (1982) 5052.
- [26] J. Keizer, J. Am. Chem. Soc. 107 (1985) 5319.
- [27] J. Keizer, Chem. Rev. 87 (1987) 167.
- [28] G.C. Joshi, R. Bhatnagar, S. Doraiswamy, N. Periasamy, J. Phys. Chem. 94 (1990) 2908.
- [29] J.B. Birks, M. Salete, S.C.P. Leite, Proc. Phys Soc. (London) 3 (1970) 417.
- [30] S. Kumar, G. Giri, S.C. Mishra, M.K. Machwe, Indian J. Pure Appl. Phys. 33 (1995) 615.