

## An Efficient implementation of PKI architecture based Digital Signature using RSA and various hash functions (MD5 and SHA variants)

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**Abstract:** Digital Signature technique is widely being used to detect unauthorized modification to data and to authenticate the identity of the signatory. It is essential for secure transaction over unsecure/ open networks. Digital Signature schemes are mostly used in cryptographic protocols to provide services like entity authentication, authenticated key transport and key agreement. The PKI (Public Key Infrastructure) based digital signature architecture is related with RSA algorithm and secure Hash functions (MD5 & SHA variants). RSA digital signature algorithm is an asymmetric cryptographic method whose security is associated with difficulty of factorization and hash function is applied to the message to yields a fixed-size message digest. This paper explores the PKI architecture based digital signature and presents an efficient way of its implementation and discusses various issues associated with signature schemes based upon RSA and hash functions. The results show that signing and verification are much faster in the developed application.

**Keywords:** Digital Signature, MD5, RSA, SHA1, SHA2

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### I. Introduction

In this fast-paced technological world the importance of information and communication systems is escalating with the increasing significance and quantity of data that is transmitted to minimize operational cost and provide enhanced services. Unfortunately the vulnerability of systems and data are highly rising due to variety of threats, such as unauthorized access and use, destruction, alteration and misappropriation. Cryptography is the foundation of all data as well as information security aspects. A digital signature is an important type of authentication in the public key cryptographic system and it is widely used around the world. (Bruce Schneier, 1996; W.C.Cheng, C.F.Chou and L.Golubchik, 2002) .

By allowing the exchange of information more quickly, easily, and dependably than ever before, the Internet has forever changed the way of business and transactions. Electronic transactions are gaining in importance as nations around the globe because of significantly reducing the need for paper documentation while providing the opportunity for tremendous efficiency and productivity gains. As a result, digital signatures are poised to enter the mainstream as primary vehicle for establishing trust for a wide variety of electronic transactions. (Burton S. Kaliski, 2001; Rivest, Shamir, & Adleman, 1978) The information handled in electronic transactions is valuable and sensitive and must be protected against tampering by malicious third parties (who are neither the senders nor the recipients of the information). Sometimes, there is a need to prevent the information or items related to it (such as date/time it was created, sent and received) from being tampered with by the sender and/or the recipient. (S. R. Subramanya and Byung K. Yi, 2006)

A digital signature is a checksum which depends on the time period during which it was produced (Denning, 1984) . It is computed using a set of rules and a set of parameters such that the identity of the signatory and integrity of the data can be verified (Biometrics: the Future of Identification, 2000).

### II. PKI ARCHITECTURE BASED DIGITAL SIGNATURE

The notion of digital signatures goes back to the beginning of public-key cryptography. In their landmark paper Whitfield Diffie and Martin Hellman (W.Diffie & M.E.Hellman, 1976) introduced the idea that someone could form a digital signature using public-key cryptography that anyone else could verify but which no one else could generate. After it RSA (Rivest, Shamir, & Adleman, 1978) has become the most proven and most popular, and achieved the widest adoption by standards bodies and in practice. (Burton S. Kaliski, 2001)

PKI is mainly used for secure transactions between companies or governmental agencies. An ecommerce Web site that uses SSL for encryption is a portion of PKI system. Encrypted e-mail is also another transaction that may be a part of a PKI system. Some companies or agencies may want all staff to digitally sign any documents they have created. Because a digital signature is derived from a Digital Certificate and its key,

this is also part of a PKI system. There are so many possible scenarios and solutions it's almost impossible to list them all (Prakash Kuppaswamy, Peer Mohammad Appa and Saeed Q Y Al-Khalidi, 2012). PKI includes the mechanics described in this article as well as an ensemble of software, hardware and processes governed by rules and standards converging to the high level of Trust required and expected by the Industry. (CGI Group Inc., 2004) The RSA public-key cryptosystem and digital signature scheme are widely deployed today and have become essential building blocks for creating the emerging public-key infrastructure (PKI). (Burton S. Kaliski, 2001) In this paper the PKI (Public Key Infrastructure) based digital signature architecture has been discussed which is related with RSA algorithm and secure Hash functions (MD5 &, SHA variants).

Basically, the idea behind digital signatures is the same as handwritten signature which are traditionally used to validate and authenticate paper documents. A major difference between handwritten and digital signature is that a digital signature cannot be constant; it must be a function of the document that is sign. (Hemant Kumar, Ajit Singh, 2012) It is used to authenticate the fact that you promised something that you can't take back later. For electronic documents, a similar mechanism is necessary. Digital signatures, which are nothing but a string of ones and zeroes generated by using a digital signature algorithm, serve the purpose of validation and authentication of electronic documents. Validation refers to the process of certifying the contents of the document, while authentication refers to the process of certifying the sender of the document. (S. R. Subramanya and Byung K. Yi, 2006)

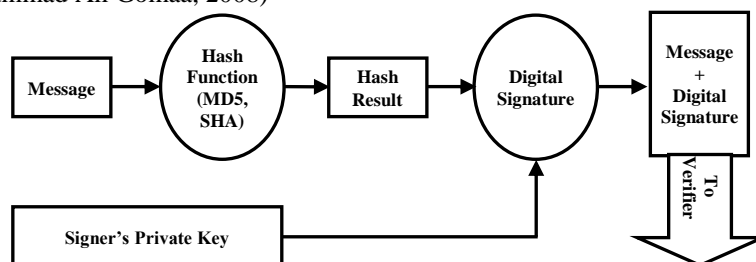
A digital signature is an electronic analogue of a written signature; the digital signature can be used to provide assurance that the claimed signatory signed the information. In addition, a digital signature may be used to detect whether or not the information was modified after it was signed i.e. to detect the integrity of the signed data. (Digital Signature Standard (DSS), June, 2009) In the situation where there is not complete trust between sender and receiver, something more than authentication is needed and the most attractive solution for this problem is the digital signature. Mainly digital signature is use in e-mail, electronic data interchange, software distribution, and other applications that require data integrity assurance and data origin authentication. The wireless protocols, like HiperLAN/2 (Martin Johnsson), and WAP (WAP Forum :), have specified security layers and the digital signature algorithm have been applied for the authentication purposes. (Hemant Kumar, Ajit Singh, 2012)

It must have some salient features such as verify the author and the date and time of signature; authenticate the contents at the time of signature; must be verifiable by third parties, to resolve disputes; it must be a bit pattern that depends on the message of being signed; must use some information unique to sender, to prevent both forgery and denial; must be relatively easy to produce to recognize and verify digital signature but computationally infeasible to forge it and must have legitimate concern.

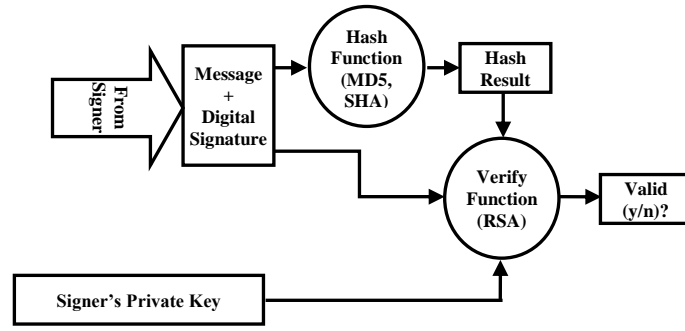
A digital signature can also be used to verify that information has not been altered after it was signed. A digital signature is an electronic signature to be used in all imaginable type of electronic transfer. Digital signature significantly differs from other electronic signatures in term of process and results. These differences make digital signature more serviceable for legal purposes.

Digital signatures are based on mathematical algorithms which includes a signature generation process and a signature verification process. A signatory uses the generation process to generate a digital signature on data; a verifier uses the verification process to verify the authenticity of the signature. These require the signature holder to have a key-pair (one private and one public key) for signing and verification. (Bruce Schneier, 1996; Rivest, Shamir, & Adleman, 1978; Digital Signature Standard (DSS), June, 2009)

Basic idea of digital signatures is each signer has a unique key called private key. There is also other part of key called public key. Whenever singer has to authenticate a document it creates a bit string called signature by applying his private key on the message or some hashed image of message as shown in Fig.1a. User who receives this message then applies his public key on the signature and checks the validity of the bit-string as shown in Fig.1b. If receiver is convinced that document is signed by legitimate signer, it accepts the document. Later if there is some dispute between sender and receiver regarding the validity of document, a third party inspects the signature and using the public key of signer verifies the signature. (Alfred J. Menezes, Paul C. van Oorschot and Scott A. Vanstone, 1997; William Stallings, Nov. 2005; Rania Salah El-Sayed, Moustafa Abd El-Aziem and Mohammad Ali Gomaa, 2008)



(a) Creating a Digital Signature



(b) Verifying a Digital Signature

Figure 1 : Generalized signature Generation and Verification

It has three phases namely (1) Key Generation (2) Signature Generation (3) Signature Verification. The Key Generation phase is the foundation phase for it.

1.1. Key-pair Generation

To generate key-pair for digital signature - RSA algorithm (Rivest, Shamir, & Adleman, 1978), most widely-used public key cryptography algorithm in the world, is used. The idea is that it is relatively easy to multiply prime numbers but much more difficult to factor. Multiplication can be computed in polynomial time where as factoring time can grow exponentially proportional to the size of the numbers. The algorithm is as follows:

- a. Select p, q such that p and q both are primes and  $p \neq q$ .
- b. Calculate  $n = p \times q$ .
- c. Calculate  $\Phi(n) = (p - 1) \times (q - 1)$ .
- d. Select integer e such that  $\text{gcd}(\Phi(n), e) = 1$  and where  $1 < e < \Phi(n)$ .
- e. Calculate  $d = e^{-1} \text{ mod } \Phi(n)$ . i.e.  $ed = 1 \text{ mod } \Phi(n)$
- f. Public key  $KU = \{e, n\}$ .
- g. Private key  $KR = \{d, n\}$ .

The Fig.2 shows the data flow diagram of key-pair generation in proposed RSAAPP.

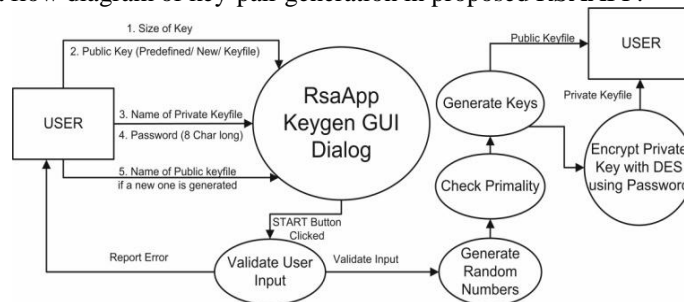


Figure 2: DFD for Key-Pair Generation in RSAAPP

1.2. Signature Generation

- a. Given a message m, we apply a suitable hash function H (MD5, SHA1 or SHA2) to obtain the hash result  $M = H(m)$ .
- b. To sign a message m, we use  $M < n$  to compute Signature  $(S) = M^d \text{ (mod } n)$  where d is the private key of the signer.

The Fig.3 shows the data flow diagram of Signature Generation in proposed RSAAPP.

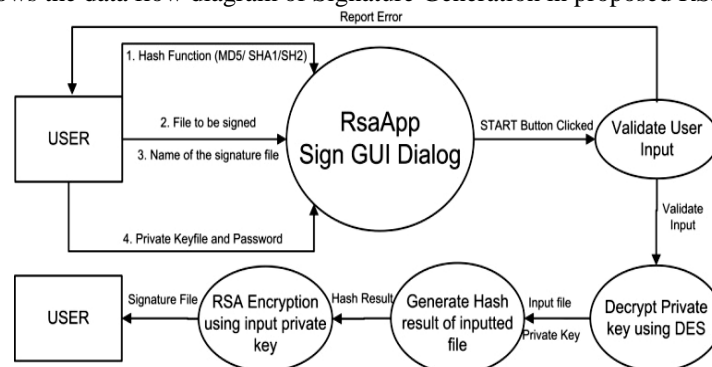
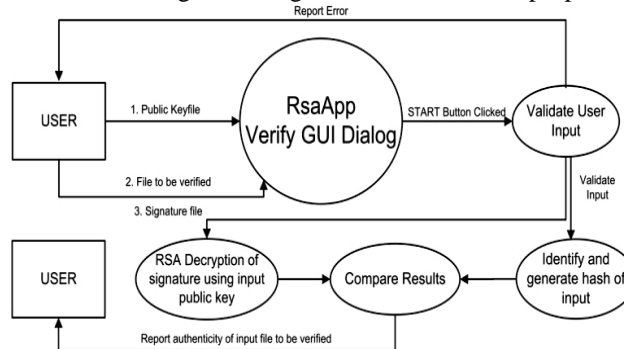


Figure 3: DFD for Signature Generation in RSAAPP

**1.3. Signature Verification**

- a. To verify the message  $m$ , we use the digital signature  $S$  to compute  $M = S^e \pmod n$  where  $e$  is the public key of the signer.
- b. Then we obtain  $M' = H(M)$  and compare it with  $M$ .
- c. If both are same then the message is authentic otherwise it is tempered.

The Fig.4 shows the data flow diagram of Signature Generation in proposed RSAAPP.



**Figure 4: DFD for signature Verification in RSAAPP**

**III. HASH FUNCTIONS (MD5, SHA1 AND SHA2)**

A typical hash function takes a variable length message and produces a fixed length hash. Given the hash, it is impossible to find a message with that hash; in fact one cannot determine any usable information about a message with that hash, not even a single bit. Hash function are used to digest or condense a message down to a fixed size, which then be signed, in a way that makes finding other messages with the same hash extremely difficult (so the signature would not apply easily to other messages). Any cryptographic hash function  $H$  has 3 important properties: (1) given message  $P$ , it is easy to compute  $H(P)$  (2) given  $H(P)$ , it is effectively impossible to compute  $P$  and (3) no one can generate two messages that have the same message digest.

**1.4. MD5 Hash Function**

The algorithm takes as input a message of arbitrary length and produces as output a 128-bit "fingerprint" or "message digest" of the input. It is conjectured that it is computationally infeasible to produce two messages having the same message digest, or to produce any message having a given prespecified target message digest. The MD5 algorithm is intended for digital signature applications, where a large file must be "compressed" in a secure manner before being encrypted with a private (secret) key under a public-key cryptosystem such as RSA. (Ronald L.Rivest) The summary of the MD5 hash function is:

$$\begin{aligned}
 F(x, y, z) &= (x \text{ AND } y) \text{ OR } ((\text{NOT } x) \text{ AND } z) \\
 G(x, y, z) &= (x \text{ AND } z) \text{ OR } (y \text{ AND } (\text{NOT } z)) \\
 H(x, y, z) &= x \text{ XOR } y \text{ XOR } z \\
 I(x, y, z) &= y \text{ XOR } (x \text{ OR } (\text{NOT } z))
 \end{aligned}$$

**1.5. SHA1 Hash Function**

NIST, along with NSA, designed the Secure Hash algorithm (SHA1) for use with the digital signature standard. The algorithm published in 1995 in FIPS PUB 180-1 is commonly referred to as *SHA-1*.

When a message of any length  $< 2^{64}$  bits is input, the SHA-1 produces a 160-bit output called a message digest. The message digest can then, for example, be input to a signature algorithm which generates or verifies the signature for the message. Signing the message digest rather than the message often improves the efficiency of the process because the message digest is usually much smaller in size than the message. The same hash algorithm must be used by the verifier of a digital signature as was used by the creator of the digital signature. Any change to the message in transit will, with very high probability, result in a different message digest, and the signature will fail to verify. (Donald E.Eastlake and Paul E.Jones, Sept. 2001) SHA-1 uses a sequence of logical functions,  $f_0, f_1, \dots, f_{79}$ . Each function  $f_t$ , where  $0 \leq t < 79$ , operates on three 32-bit words,  $x, y$ , and  $z$ , and produces a 32-bit word as output. The function  $f_t(x, y, z)$  is defined as follows: (Secure Hash Standard, United States of America, National Institute of Science and Technology, Federal Information Processing Standard (FIPS) 180-1, April 1993)

$$f_t(x, y, z) = \begin{cases} \text{Ch}(x, y, z) = (x \text{ AND } y) \text{ OR } ((\text{NOT } x) \text{ AND } z) & (0 \leq t \leq 19) \\ \text{Parity}(x, y, z) = x \text{ XOR } y \text{ XOR } z & (20 \leq t \leq 39) \\ \text{Maj}(x, y, z) = (x \text{ AND } y) \text{ OR } (x \text{ AND } z) \text{ OR } (y \text{ AND } z) & (40 \leq t \leq 59) \\ \text{Parity}(x, y, z) = x \text{ XOR } y \text{ XOR } z & (60 \leq t \leq 79) \end{cases}$$

1.6. SHA2 Hash Function

In 2005, cryptanalysts found attacks on SHA-1 suggesting that the algorithm might not be secure enough for ongoing use. (Bruce Schneier, 2005) NIST required many applications in federal agencies to move to SHA-2 after 2010 because of the weakness.

SHA-2 is a set of cryptographic hash functions (SHA-224, SHA-256, SHA-384 and SHA-512) designed by the U.S. National Security Agency (NSA) and published in 2001 by the NIST as a U.S. Federal Information Processing Standard (FIPS) PUB 180-2. But in the proposed RSAAPP we use SHA-256.

SHA-256 uses six logical functions, where each function operates on 32-bit words, which are represented as x, y, and z. The result of each function is a new 32-bit word. (Secure Hash Standard, United States of America, National Institute of Science and Technology, Federal Information Processing Standard (FIPS) 180-2, 2002)

$$Ch(x, y, z) = (x \wedge y) \oplus (\neg x \wedge z)$$

$$Maj(x, y, z) = (x \wedge y) \oplus (x \wedge z) \oplus (y \wedge z)$$

$$\sum_0^{[256]}(x) = ROTR^2(x) \oplus ROTR^{13}(x) \oplus ROTR^{22}(x)$$

$$\sum_1^{[256]}(x) = ROTR^6(x) \oplus ROTR^{11}(x) \oplus ROTR^{25}(x)$$

$$\sigma_0^{[256]}(x) = ROTR^7(x) \oplus ROTR^{18}(x) \oplus SHR^3(x)$$

$$\sigma_1^{[256]}(x) = ROTR^{17}(x) \oplus ROTR^{19}(x) \oplus SHR^{10}(x)$$

IV. THE DEVELOPED APPLICATION (RSAAPP)

To test and compare the performance characteristics of the RSA and discussed signature algorithms, we developed application RSAAPP using C language with windows API (Charles Petzold, Nov. 1998). The key generation process generates the public and private keys in pairs. If required the keys can be viewed in hex format after generation. The corresponding private keys generated are encrypted using DES after taking an 8-character password as user input. The proposed application can be used encrypt any kind of data i.e. text or binary. It uses SHA2, SHA1 and MD5 hash algorithms for the digital signature. SHA2 is much more secure than SHA1 and MD5. After key generation the Signature Generation module is processed for the file which is to be signed by the signer and sent to the recipient. Further at the receiving end the recipient verifies the signature by execution of Signature Verification process to authenticate that the file has been sent by the authentic sender and to validate that the file has been tampered or not. The figures below shows the execution of the developed application i.e. RSAAPP-

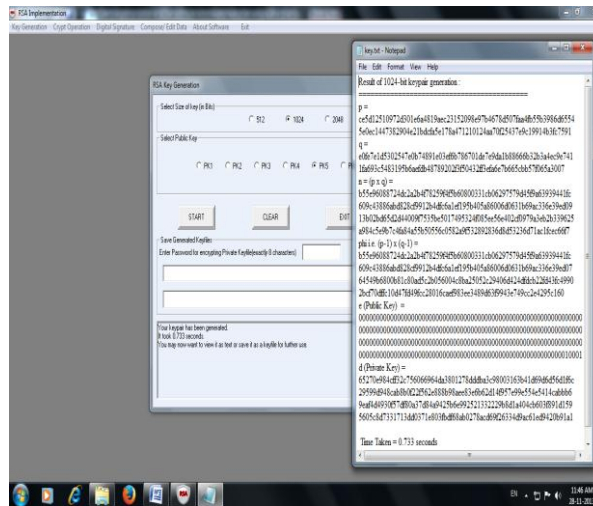
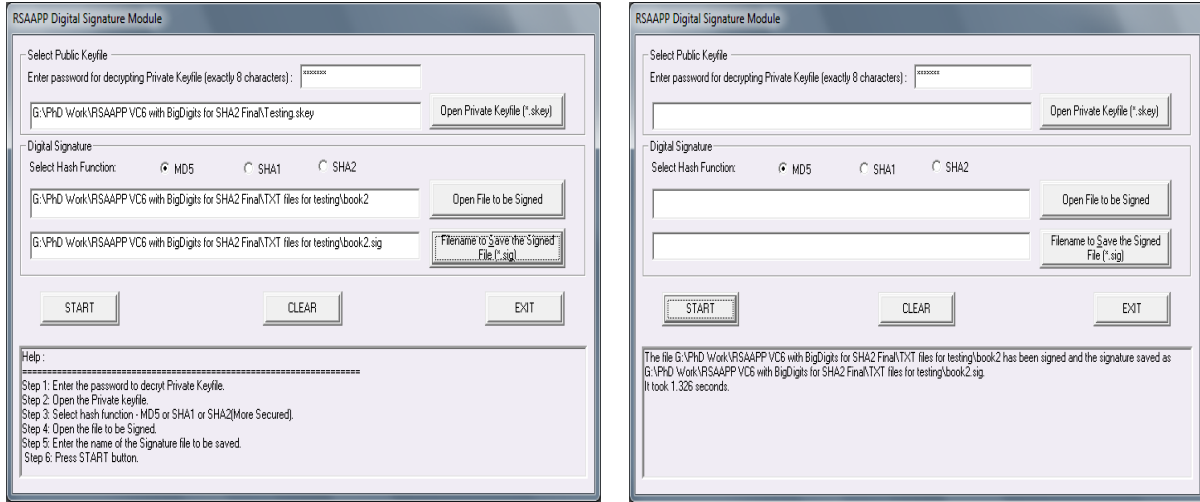


Figure 5: Result of the Key Generation



(a) Signature Generation module of RSAAPP

(b) Completion of Signature Generation of RSAAPP

Figure 6: Signature Generation module of RSAAPP

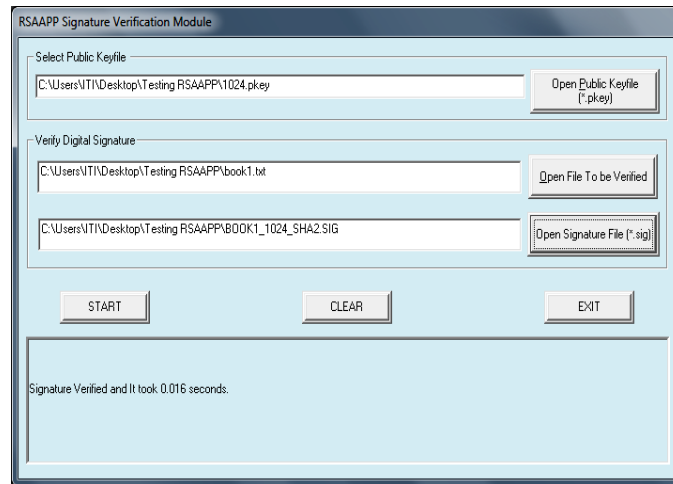


Figure 7: Signature Verification module of RSAAPP

## V. EXPERIMENTAL RESULTS

The test results of the developed program RSAAPP for signature generation and signature verification using MD5, SHA1 and SHA2 are tabulated in seconds as shown in Table1. Three files of different size are chosen randomly from Calgary Corpus (Ian Witten, Timothy Bell and John Cleary, 2013) which is a collection of text and binary data files. Tests are performed on an Intel P4 1.7GHz machine with 1GB of RAM with key size 1024 bits. Time taken in RSA 1024 bit key generation is 2.2 seconds. The experiment results with MD5, SHA1 and SHA2 hash functions are tabulated in seconds as shown in Table1.

Table 1: Experimental Results

Filename with size	MD5		SHA1		SHA2	
	Sign. Gen.	Sign. Verify	Sign. Gen.	Sign. Verify	Sign. Gen.	Sign. Verify
paper4 (12.9 KB)	0.381	0.02	0.381	0.03	0.481	0.02
news (368 KB)	0.430	0.04	0.511	0.05	0.411	0.03
book1 (596 KB)	0.461	0.06	0.571	0.06	0.421	0.06

## VI. CONCLUSION

The experimental results shows that the RSA key (1024 bits), signature generation and signature verification with different hash functions – MD5, SHA1 and SHA2 are quite fast in developed RSAAPP. The cost of signature generation can be considered as a factor in the choice of signature system. The developed RSAAPP system achieves high security for digital signature in addition to decrease processing time and computational overheads. And an intruder cannot pose the message sent since the sender's private key is unknown for him. Accordingly, the sender cannot be impersonated. On the receiver part, the message is verified by using sender's public key and his private key to decrypt the message successfully.

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