

Medical Image De-Noising Using Hybrid Methodology with Wavelets and Guided Filter

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Abstract: Image DE-noising is an important part of image processing and computer vision problems. One of the most powerful and perspective path in this area is image de-noising using discrete wavelet transform (DWT) and guided filters. This paper prefer a new image de-noising method using hybrid methodology which gives better performance than the DWT and guided filters. The DE-noised image performance can be evaluated in terms of peak signal to noise ratio (PSNR), Mean Squared Error (MSE), Correlation Coefficient. The proposed work will be implemented using MAT LAB R 2015a.

Keywords: DWT, Guided filter, MSE, PSNR, Correlation Coefficient

I. Introduction

The Images are corrupted with noise modeled with either a Gaussian, uniform, Rician, or salt and pepper distribution. Neither the typical noise is a speckle noise, which is multiplicative in nature. The Speckle noise is observed in ultrasound images, whereas Rician noise affects MRI images. Mostly, noise in digital images is found to be additive in nature with uniform power within the whole bandwidth and with Gaussian probability distribution. This a noise is referred to as Additive White Gaussian Noise (AWGN). White Gaussian noise is being caused by poor image acquisition or by transferring the image data in noisy communication channel. Most de-noising algorithms use images artificially distorted by well-defined white Gaussian noise to achieve objective test results.

A hybrid de-noising algorithm that combines wavelet thresholding and guided filter is proposed. Discrete wavelet transform is used to decompose the noisy image and step towards its different sub bands namely LL, LH, HL, and HH. Soft thresholding is applied over sub bands (LH, HL and HH) to de-noise the image. The Inverse discrete wavelet transform is applied to retrieve the de-noised image but still it is having a minute noise, another guided filter is applied tend to cancel residual noise components if any.



Fig.1. Flowchart of proposed methodology

Noise

In general the Noise is introduced in the image at the time of image acquisition or transmission. Individual factors may be culpable for introduction of noise in the image. The number of pixels perverted in the image will decide the quantification of the noise. The principal origin of noise in the digital image are:

- The imaging sensor may be influenced by environmental terms conditions during image acquisition.
- The noise in the medical image can be altering by presentation of inadequate Slight levels and sensor temperature.
- Medical image may be corrupted by interference in the transmission.
- The introduction of noise in the medical image due to the dust particles are presents on the scanner screen.

II. Gaussian Noise

Gaussian noise is identically distributed over the signal. Already stated that each pixel in the noisy image is the totally true pixel value and a random Gaussian distributed noise value. As the name suggest, this type of noise has a Gaussian distribution, that has a bell shaped probability distribution function given by,

$$F(g) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(g-m)^2}{2\sigma^2}}$$

Where g represents the gray level, m is the mean or average of the function and σ is the standard deviation of the noise. Graphically, it is represented as shown in Figure 2 When imported into an image, Gaussian noise with zero mean and variance as 0.05 would look as in Image 2.1. Image 2.2 illustrates the Gaussian noise with mean (variance) as 1.5(10) over a base image with a constant pixel value of 100.

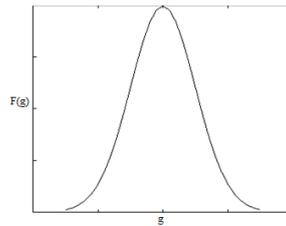


Fig.2 Gaussian distribution

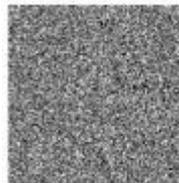


Image 2.1 Gaussian noise
(Mean = 0, variance = 0.05)



Image 2.2 Gaussian noise
(Mean = 1.5, variance = 10)

III. Wavelet Thresholding

Wavelet Thresholding is very simple non-linear method, which concern on one wavelet coefficient at a time. In general, each coefficient is threshold by compare with respect to threshold, if the coefficient is smaller than threshold, set to zero; or else it is kept or modified [2]. Transforming the all small noisy coefficients by zero and inverse wavelet transform on the result may guide to reconstruction with the essential signal characteristics and with less noise. Wavelet thresholding suggest threes steps a linear discrete wavelet transform, nonlinear thresholding Step & a linear inverse wavelet transform [5]. Let us estimate a signal $\{x_{ij}, i, j = 1, 2, \dots, N\}$ denote the $N \times N$ matrix of the original image to be retrieved and N is some integer power of 2. Throughout transmission the signal is corrupted by independent and equally distributed zero mean, white Gaussian Noise z_{ij} with standard deviation σ i.e. $z_{ij} \sim M(0, \sigma^2)$ as follows. $Y_{ij} = X_{ij} + Z_{ij}$ From this noisy signal y , we want to find a correlate x_{ij} . The goal is to analyze the signal X_{ij} from noisy observations y_{ij} this Mean squared error (MSE) is minimum. I.e.

$$\|X - \bar{X}\|^2 = 1/M \sum_{l=0}^{N-1} (X_l - \bar{X}_l)^2$$

Let W and W^{-1} denote the two-dimensional orthogonal discrete wavelet transform (DWT) Matrix and its IDWT resultantly. Then equation (1) can be written as

$$d_{ij} = c_{ij} + \varepsilon_{ij}$$

With $d=W y$, $c =W x$, $\varepsilon =W z$. Since W is orthogonal transform, ε_j is also an i.e. Gaussian random variable with $i,j \sim (0, \sigma^2)$. Now $T(\cdot)$ be the wavelet thresholding function then the wavelet thresholding based De-noising scheme can be expressed as $X = W^{-1}(T(Wy))$ wavelet transform of noisy signal should be taken first and then thresholding function is applied on it. Totally the output should be undergone inverse wavelet transformation to secure the estimate x . There are two thresholds frequently used, i.e. hard threshold, soft threshold. The hard thresholding function is described as

$$f_h(x) = \begin{cases} x & \text{if } |x| \geq \lambda \\ 0 & \text{otherwise} \end{cases}$$

The hard-thresholding function chooses all wavelet coefficients that are greater than the given threshold λ and sets the others to zero. The threshold λ is chosen suitable to the signal energy and the noise variance (σ^2).

The soft-thresholding function has a significantly different rule from the hard-thresholding function. It adequately the wavelet coefficients by λ towards zero,

$$f_s(x) = \begin{cases} x - \lambda & \text{if } x \geq \lambda \\ 0 & \text{if } |x| < \lambda \\ x + \lambda & \text{if } x \leq -\lambda \end{cases}$$

The soft-thresholding rule is chosen over hard-thresholding, for the soft-thresholding method Yields more graphically pleasant images over hard thresholding [6].

Already we arrive at our discrete wavelet coefficients; we need a way to recreate them back into the original image (or a modified original image if we played around with the coefficients). In sequences to do this, we accept the process known as the inverse discrete wavelet transform. Practically the DWT can be explained by using filter bank theory, so can the reconstruction of the IDWT. The process is simply reversed [7]. The DWT coefficients are first up specimen by placing zeros in between every coefficient, exclusively doubling the lengths of each. These are then convolute with the recreate scaling filter for approximation coefficients and the recreate wavelet filter for the detail coefficients. These results are then added together to appear at the original image. Alike to how we made the image recurring before doing our DWT calculations on it, we must make our dwt coefficients periodic before convoluting to secure the original image. This is done by commonly taking the first N/2-1 coefficients from the DWT coefficients, and conjoins them to the end.

IV. Guided Filter

In sequences to overcome the artifacts[3] introduced by bilateral filter, a new edge preserving performance known as guided image filter is proposed that execute edge-preserving smoothing on an image, using the content of the second image i.e. the guidance image, in sequences to influence the filtering. The guidance image can be the image itself, an individual version of the image or a completely various image. If the guidance image is like as the input image to be filtered, the structures are the equivalent i.e. an edge in original image is the like as in the guidance image.

Guided image filtering is one of the spatial domain enhancement method and that the filtering output is locally a linear Transform of the guidance image. It takes through account the statistics of a region in the comparable spatial neighborhood in the Guidance image while considerate the value of the output pixel. Guided filter has good edge-preserving smoothing properties and do not suffer from the gradient reversal artifacts that are seen when using bilateral filter. It can execute better at the pixels nearby edge when related to bilateral filter. The guided filter is also a more generic concept after smoothing [1]. By taking the guidance image, it makes the filtering output more structured and less smoothed than the input. It can deportation the structures of the guidance image to the Filtering output, enabling new filtering applications that dehazing and guided feathering. Also, guided filter adopts the fast and Non-approximation characteristics of linear time algorithm and produce an ideal option for real time applications in case of HD Filtering. Hence, it is treated to be one of the fastest edge preserving filters. Guided filter generally has an O(N) time (in the number of pixels N) exact algorithm for the two gray scale and color images, Regardless of the kernel size and the range of intensity. O(N) time show that the time complexity is independent of the window radius(r) and hence arbitrary kernel sizes can be used in the applications.

4.1 Definition:

Here, the main concept and equations of a guided filter is considered. The key assumption of the guided filter defines a local linear model within the guidance image I and the filtered output image q, taking p as an input image as shown in fig.1 which shows an illustration of the guided filtering process.

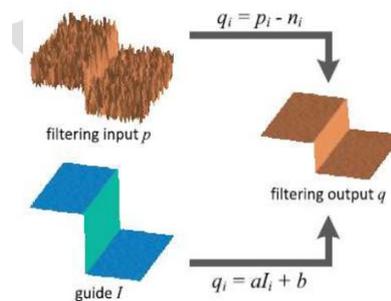


Fig. 3 Illustration of guided filtering process

It is pretended that q is a linear transform of I in a window w_k , that is centered at pixel k.

$$q_i = a_k I_i + b_k \forall i \in w_k. \tag{1}$$

where, a_k and b_k are treated to be linear coefficients that are constant in w_k . A square window of radius r is used. The relation is shown in fig.3. This local linear model ensures that q has edge only if I have edge.

In sequences to determine the linear coefficients (a_k, b_k), we need constraints from the filtering input p. We model the output q as the input p subtracting some undesirable components n like noise/textures:

$$q_i = p_i - n_i \tag{2}$$

$$a_k = \frac{\frac{1}{|w|} \sum_{i \in w_k} I_i p_i - \mu_k \overline{p_k}}{\sigma_k^2 + \epsilon} \tag{3}$$

$$b_k = \overline{p_k} - a_k \mu_k \tag{4}$$

Where, μ_k is the mean whereas σ_k^2 is the variance of I in window w_k and $||$ is the number of pixels in window w_k .

Also, $\overline{p_k} = \frac{1}{|w|} \sum_{i \in w_k} p_i$ is the mean of p in window w_k . After secure the linear coefficients (a_k, b_k) , we can compute the filtering output q_i from equation 4. Since a pixel i is elaborate in all the overlapping windows w_k that will cover I and hence the value of q_i in (4) does not remain same when computed in different windows. A solution is to average all the possible values of q_i . Therefore, after measure the linear coefficients for all the windows w_k in the image, we can compute the filtering output by:

$$q_i = \frac{1}{|w|} \sum_{k \in w_i} a_k I_i + b_k \tag{5}$$

As the symmetry of the box window, we rewrite (5) by

$$q_i = a_{i1} I_i + b_{i1} \tag{6}$$

Where, $a_{i1} = \frac{1}{|w|} \sum_{k \in w_i} a_k$ and $b_{i1} = \frac{1}{|w|} \sum_{k \in w_i} b_k$ are the average coefficients of all the windows overlapping i . As (a_{i1}, b_{i1}) are the output of a mean filter, the gradients secure from them can be expected to be very much smaller than that of the guidance image I near strong edges. This situation ultimate that abrupt intensity changes in I can be preserved in q mostly. Hence, (3), (4), (6) shows the definition of the guided filter.

V. Results

Mean square error (MSE):

Speckle noise variance	Guided filter	Dwt soft thresholding	Guided + soft thresholding	Dwt soft thresholding + guided filter
0.1	34.0262	28.1935	28.0197	18.7244
0.2	40.7423	35.2809	35.3687	25.1517
0.3	43.8762	38.9040	39.0602	29.9774

Peak signal to noise ratio (PSNR):

Speckle noise variance	Guided filter	Dwt soft thresholding	Guided + soft thresholding	Dwt soft thresholding + guided filter
0.1	32.8127	33.6293	33.6526	35.4067
0.2	32.0304	32.6554	32.6446	34.1251
0.3	31.7085	32.2309	32.2135	33.3629

Correlation and coefficients:

Speckle noise variance	Guided filter	Dwt soft thresholding	Guided + soft thresholding	Dwt soft thresholding + guided filter
0.1	0.9400	0.9601	0.9590	0.9791
0.2	0.8849	0.9241	0.9214	0.9568
0.3	0.8369	0.8900	0.8861	0.9305

Structure similarly index:

Speckle noise variance	Guided filter	Dwt soft thresholding	Guided + soft thresholding	Dwt soft thresholding + guided filter
0.1	0.7749	0.8132	0.8119	0.8713
0.2	0.7030	0.7425	0.7391	0.8141
0.3	0.6660	0.7016	0.6979	0.7663



(a). Liver image effected by speckle nose with noise variances 0.3
(b). image de-noise by proposed method.

VI. Conclusion

Hybrid combination of dwt soft thresholding and guided filter is proposed to de-noise the medical images suffered with speckle noise. The proposed method results show excellence performances. In this paper compare the results in different variance with dwt, guided filter individually and guided + soft thresholding combinations performances measures are MSE, PSNR, COC, and SSIM.

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