

Solution of Unit Commitment Problem Using Shuffled Frog Leaping Algorithm

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ABSTRACT: This paper presents a solution to Unit commitment (UC) of thermal units based on a new evolutionary algorithm known as Shuffled Frog Leaping Algorithm(SFLA). The integer coded algorithm is based on the behavior of group of frogs searching for a location that has the maximum amount of available food. This algorithm involves local search and shuffling process and these are repeated until a required convergence is reached. In this proposed method of SFLA for the UC problem, the scheduling variables are coded as integers, so that the minimum up/down time constraints can be handled directly. To verify the performance of the proposed algorithm it is applied to the IEEE 14, 30, 56,118 bus systems and 10, 20 unit systems for a one day scheduling period. The results obtained are quite encouraging for the Unit Commitment problem when compared with the existing methods. The algorithm and simulation are carried out using Matlab software.

Key words: SFLA ,Frogs, Unit Commitment

Abbreviations:

T -Time horizon of Unit commitment (hrs)
 P_D^t - Real power demand at t^{th} hour (MW)
 P_i - Real power generation of i^{th} Unit (MW)
 X_i - Commitment Status of i^{th} Unit
 P_{imax} - Maximum real power generation of i^{th} Unit (MW)
 P_{imin} - Minimum real power generation of i^{th} Unit (MW)
 SUC_i - Start- up cost of i^{th} unit (\$)
 RD_i - Allowable change in real power of i^{th} unit
 DT_i - Shut down duration of i^{th} unit(hrs)
 MDT_i - Minimum down time of i^{th} unit (hrs)
 MUT_i - Minimum up time of i^{th} unit (hrs)
 HSC_{i1} -Hot startup cost of i^{th} unit (\$)
 CSC_i - Cold start up cost of i^{th} unit (\$)
 CSH_i - Cold start hour of i^{th} unit(hrs)
 N -No., of generating units
 C - No.,of cycles
 T_i^c - Duration of c^{th} cycle of i^{th} unit (hrs)

I. INTRODUCTION

Operating under the present competitive environment, Unit Commitment (UC) is essential since a significant amount of savings can be obtained by a sound UC decision. UC is a process of determining the minimal production cost generator turn ON/turn OFF schedule and real power outputs of committed units while meeting the forecasted demand over a scheduling horizon of usually between 24hrs to 168hrs (1 day- 7 days). The obtained UC schedule should also satisfy the global constraints (power balance, spinning reserve and environmental) and local constraints like operational and physical constraints of every unit [1][2]&[3]. Since it has to satisfy more number of constraints the UC Problem is a complex, non-linear, mixed integer optimization problem. UCP's combinatorial nature curtails any attempt to develop a rigorous mathematical optimization method.

Mathematical solution to UCP involves simultaneous solution of two sub problems. (i) The mixed integer non-linear programming problem of determining the generating units to be committed each hour of the planning horizon, while considering system capacity requirements. (ii)The quadratic programming problem of economic dispatch among the committed units during every specific hour of operation.

Complete enumeration can give an optimal solution but its excessive computational complexity has made it not suitable for large scale system.

In Literature there exist more no of methods to solve UCP [4]. The available approaches may be (i) numerical solution techniques such as Priory List (PL), Dynamic programming (DP) [5], Lagrangian relaxation, Branch and bound, and MIP. The PL is simple and fast but always led to a solution of higher operating cost. DP suffers with the problem of sub optimal solution while truncating some of the non-feasible solution, to reduce its computational time.

LR [6] is modifiable to the model characteristics of specific utilities of power system. The constraints can be easily added to the main objective function but the major drawbacks are its sensitivity and the availability of dual optimal solution. (ii) The stochastic search methods such as Genetic Algorithm (GA), [7], [8]&[9], Particle Swarm Optimization (PSO)[11], Ant colony optimization, and Bacterial foraging (BF)[13] . These methods are capable of handling complex nonlinear constraints to provide a high quality solution. GA suffers with long computation time due its random selection of GA operator. Integer coded GA for UC is more efficient than binary coded when accompanied by a suitable GA operator. Evolutionary programming (EP) differs from GA from the method of solution coding and selection of candidates for reproduction.

Eusuff and Lansey first introduced SFLA [14],[15]&[16] in 2003. This method is based on the behavior of frogs search for the location that has the maximum amount of available food. Possible solutions are randomly generated to create the initial population of frogs. And these frogs are grouped into memplexes. Memetic evolution step (local search) is carried out within every memplex and a shuffling is done between the memplexes. This process is repeated till a required convergence is reached. This algorithm has been successfully applied for several engineering optimization problems.

The integer coded UC [10] is used. The minimum up/down constraints are directly coded hence no need for any penalty function for these constraints. The performance of this algorithm is tested for a 10 unit system for a one day scheduling.

II. MATHEMATICAL MODELING OF UC

The total operating cost of electrical energy includes fuel cost, start up cost and shut down cost. The fuel costs are calculated using the data of unit heat rate & fuel price information which is normally a quadratic equation of power output of each generator at each hour determined by Economic Dispatch(ED).

$$F_c(P_i) = A_i + B_i P_i + C_i P_i^2 \quad (1)$$

Where, A_i, B_i, C_i are coefficients of cost matrix.

The total fuel cost for the entire scheduling horizon 'T' is given by

$$TFC = \sum_{t=1}^T \sum_{i=1}^N F_c P_i * X_i(t) \quad (2)$$

Where $X_i(t)$ is the status of i^{th} unit at t^{th} .hour. Startup cost is the cost involved in bringing the thermal unit online. Start up costs are expressed as a function of the number of hours the units has been shut down. (exponential when cooling and linear when banking). Shut down costs are defined as a fixed amount for each unit/shutdown. However it is not taken into account in this paper. A simplified start up cost model is used as follows.

$$SUC_i = \begin{cases} HSC_i, & \text{if } MDT_i \leq DT_i < MDT_i + CSH_i \\ CSC_i, & \text{if } DT_i > MDT_i + CSH_i \end{cases} \quad (3)$$

DT_i is the shut down duration, MDT_i - Minimum down time, HSC_i -Hot startup cost, CSC_i - Cold start up cost, and CSH_i is the Cold start hour of i^{th} unit.

There are several constraints that must be satisfied by the UCP.

i) System power balance

The sum of generation of all the committed units at t^{th} hour must be greater than or equal to the demand at a particular hour 't'.

$$\sum_{i=1}^N X_i(t) P_i(t) \leq P_D(t), \quad t = 1,2,3 \dots \dots T \quad (4)$$

ii) System spinning reserve requirements

In order to maintain certain degree of reliability an excess capacity of generation is essential to immediately take over when a running unit fails, or unexpected load occurs. A fixed reserve policy is used in this paper and a the mathematical equation is given by

$$\sum_{i=1}^N X_i(t) P_i(t) \leq P_D(t) P_R(t), \quad t = 1,2,3 \dots \dots T \quad (5)$$

iii) Min up/down time

A committed unit can be turned off only after it satisfies its minimum up time values, at the same time, a reserved unit can be turned on only after it satisfies, its min down time. This is due to the fact that the temperature of a thermal unit can be increased or decreased only gradually.

$$\begin{cases} T_i^c \geq MUT_i \text{ if } T_i^c > 0 \\ -T_i^c \geq MDT_i \text{ if } T_i^c < 0 \end{cases} \quad (6)$$

where T_i^c is a signed integer representing ON/OFF status duration of c^{th} operating cycle of the i^{th} unit .

iv) Initial operating status of generating units

The initial operating status of every unit should take the last day's previous schedule into account, so that every unit satisfies its minimum up/down time.

v) Maximum/Minimum power limits

Every unit has its own maximum/minimum power level of generation, beyond and below which it cannot generate.

$$P_{imin} \leq P_i^t \leq P_{imax} \quad (7)$$

vi) Ramp rate constraints

Since, the temperature of a thermal unit can only be increased or decreased gradually, the output also can be increased or decreased within a limit. The response rate constraints of the unit limits the power generation and is given by

$$\begin{aligned} P_{imax}(t) &= \min(P_{imax}, P_{i(t-1)} + \tau RD_i) \\ P_{imin}(t) &= \max(P_{imin}, P_{i(t-1)} - \tau RD_i) \end{aligned} \quad (8)$$

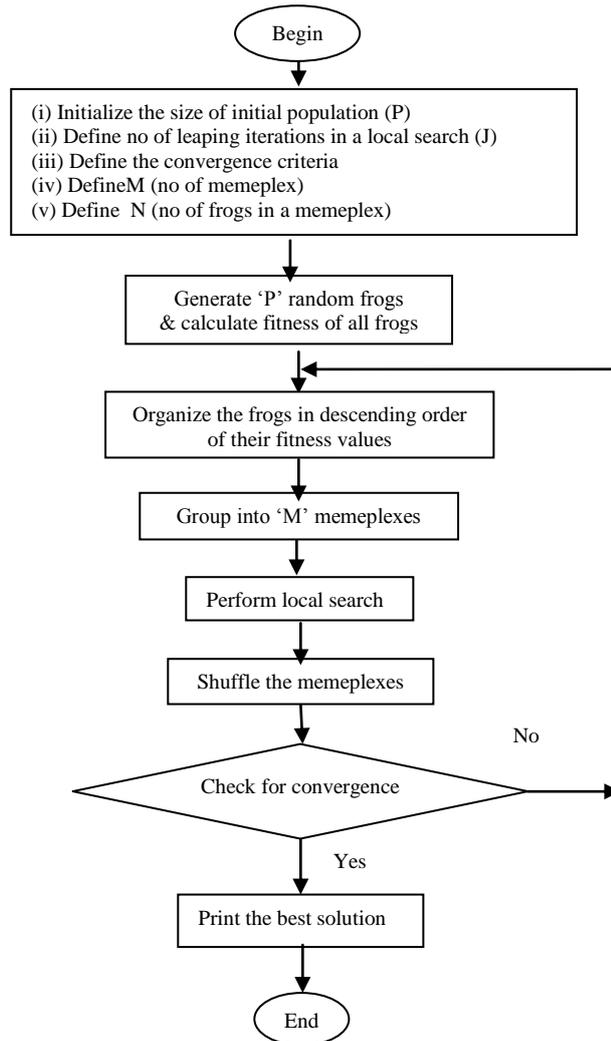
Where $\tau=60$ min.

III. SHUFFLED FROG LEAPING ALGORITHM

SFLA is a metaheuristic optimization method which combines the GA's memetic evolution and PSO's social behavior. It is a combination of deterministic and random strategies. The deterministic approach allows the algorithm to use the search space effectively to guide its heuristic search and the random approach ensures flexibility and robustness of the search process. SFLA mainly based on the behavior of group of frogs searching for the location that has the maximum amount of available food. This algorithm is capable of solving discrete and continuous optimization problems. It is also capable of solving non-linear non-differentiable, multi modal optimization problems. This algorithm has been successfully applied for several engineering applications like bridge deck repair, water source distribution, determination of optimal discrete pipe size for new pipe networks, data clustering, job shop scheduling etc, The most promising benefit of this algorithm is its faster convergence speed.

The SFLA involves a population of possible solutions defined by a set of virtual frogs. This set of virtual frogs is partitioned into subsets know as memeplexes. The memeplexes can be perceived as a set of parallel frog cultures attempting to reach some goal. Frog leaping improves an individual frog and enhances its performance towards the goal. Within each memeplex each frog holds different ideas and the idea of each frog can be used to infect the ideas of other frogs.

The process of passing information between the frogs of a memeplex is known as local search or memetic evolution step. After a defined number of memetic evolution step the virtual frogs are shuffled and reorganized so that the quality of memeplex is improved. Shuffling enhances the meme quality after infection and ensures the cultural evolution towards any particular interest. The process of memetic evolution and shuffling are repeated unit a required convergence is reached. This is given graphically in Fig.1. The following steps are involved in SFLA.



Fig(1) Flow Chart of SFLA

Step:I Formation of Initial population

- 1) Population size (no. of frogs)P is chosen
- 2) P no. of frogs are generated randomly within the search space.
- 3) The position of every frog is defined as

$$X_i = X_{i1}, X_{i2}, \dots, \dots, \dots, X_{iD},$$
 Where D is the no. of variables

4) The fitness of search frog is calculated as

$$fitness = \begin{cases} 1/f(x) + c & \text{for minimization problems} \\ f(x) + c & \text{for maximization problems} \end{cases} \quad (9)$$

f(x) is the objective function and c is a constant to ensure the fitness a positive value.

Step:II Grouping of Frogs into Memplexes:

- 1) The frogs are sorted in descending order according to their fitness values.
- 2) The entire population of 'P' frogs are grouped into 'M' memplexes, and each memplex is formed so that each memplex consists of 'N' no of frogs (P=MXN).
- 3)The partitioning of memplexes is done so that each memplex have frogs with lower and higher fitness values. For this the first frog goes to 1st memplex, the second frog goes to 2nd memplex, the mth frog to mth memplex and m+1th frog goes to 1st memplex. This procedure is illustrated in Fig.2.

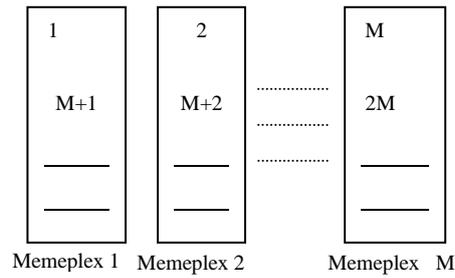


Fig. 2. Formation of Memplexes

Step: III Local search process: (Memetic evolution step)

Within each memplex, the frogs with worst (X_w) & best (X_b) fitness values are identified. Also the frog with global fitness X_g is also identified.

- 1) The frog with worst fitness is leaped towards the best frog by a random vector.

$$D_i = rand(1) * (X_b - X_w)$$

$$X_w = X_w + D_i \quad D_{imin} < |D_i| < D_{imax} \tag{10}$$

- 2) The fitness of the new leaped worst frog is calculated. If there is no improvement in fitness, the leaping vector is calculated with X_g

$$D_i = rand(1) * (X_g - X_w)$$

$$X_w = X_w + D_i \quad D_{imin} < |D_i| < D_{imax} \tag{11}$$

- 3) The fitness of the new leaped worst frog is calculated. If there is no improvement, then X_w is replaced with a new random frog. This is illustrated in Fig. 3.

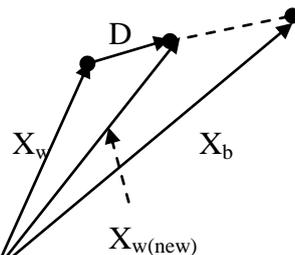


Fig.3. Frog Leaping Rule

The steps 1, 2, 3, & 4 are repeated for some specific number of iterations. The entire process of local search is illustrated graphically in fig 4.

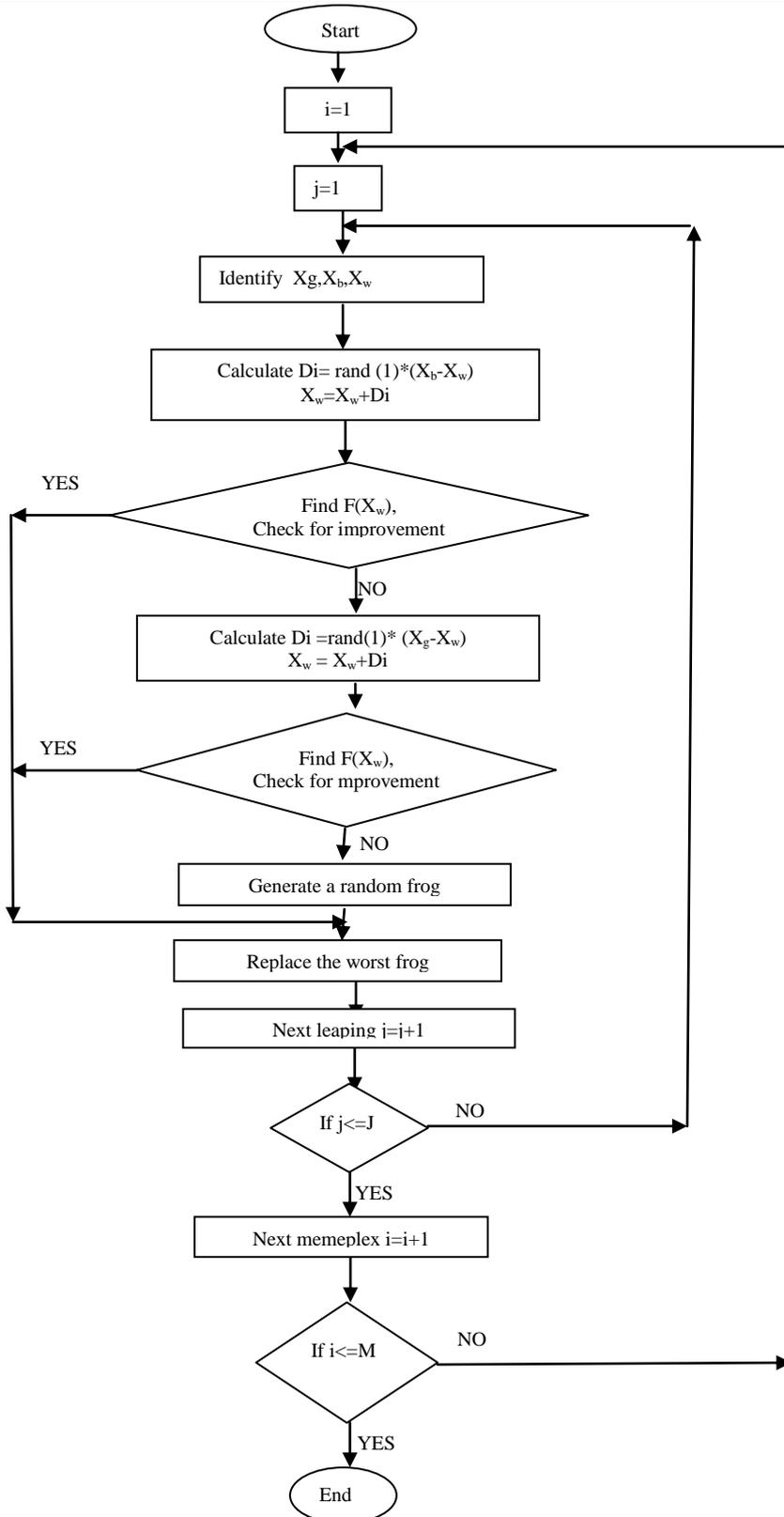


Fig.4. Local Search Process of Improved SFLA

Step: IV Shuffling Process:

After local search in every memplex is completed shuffling of memplex is done, and the frogs are reorganized in descending order of fitness values and again grouped into memplex and local search process is carried out.

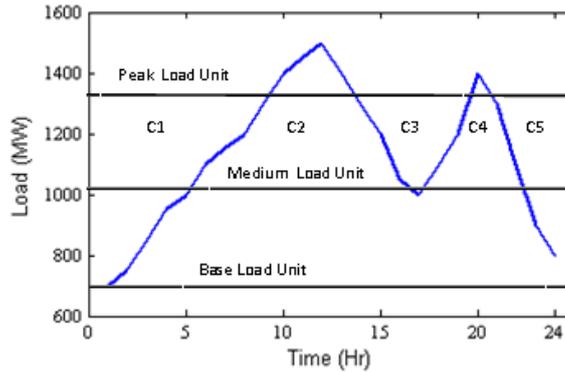
Step: V The above all steps I, II, III, IV are repeated until

- i) The relative change in the fitness of the global frog within a number of consecutive shuffling iterations is less than a pre-specified tolerance.
- ii) The maximum predefined numbers of shuffling iterations have been reached.

IV. IMPLEMENTATION OF SFLA TO UCP

Definition of frog position

The position of a frog in integer coded SFLA for UCP consists of a sequence of alternatively signed integers representing the duration of ON/OFF cycles of units during the scheduling horizon. A positive integer in the frog vector represents the duration of continuous ON state of a unit whereas the negative integer represents the duration of continuous OFF state of a unit. The size of a frog is decided by the no of units (N) and no of cycles(C). No of cycles(C) is determined by the load peaks and minimum up and down time of units



Fig(5) Load Curve for 24 Hrs

In this paper the load profile with two load peaks fig(3) is considered. From the figure it is understood that the peak units will have 5 cycles and the base units and intermediate units will have 1&3 respectively. So, the no of cycles vary between 1 to 5. But for simplicity and to increase the search space, the peaking unit cycles are taken for base and intermediate units and their remaining cycles are assumed to be zero. For a 10 unit, 5 cycle system the size of the frog for a one day scheduling is 1X10X5. Definition of frog from ON/OFF cycle duration of units and the UC schedule is illustrated in table :1

Creating Initial Population

A part of a frog representing the operating schedule of a particular unit during the scheduling horizon should be formed such that $\sum_{c=1}^C |T_i^c| = T$.

The values of T_i^c of the initial population is randomly generated as follows.

Formation of first cycle: (T_i^1)

T_i^1 is selected so that the unit continues the operating mode(ON/OFF) of the last cycle of the previous day scheduling (T_i^0) for at least as many hours required so that no units are violating its minimum up/down time values.

$$T_i^1 = \begin{cases} +rand(\max(0, MUT_i - T_i^0), T) & \text{if } T_i^0 > 0 \\ -rand(\max(0, MDT_i + T_i^0), T) & \text{if } T_i^0 < 0 \end{cases} \quad (12)$$

Formation of in between cycles ($T_i^c, 1 < c < C$)

The cycles between the initial and last cycles are generated considering the units minimum up/down time, the scheduling horizon(T) and the duration of previous cycles(i.e) duration of (c-1) prior cycles.

If $T_i^{c-1} < 0$, indicates cycle 'c' is positive and it represents an ON status of i^{th} unit.

$$T_i^c = \begin{cases} +rand(MUT_i, RT_i^{c-1}), & \text{if } (RT_i^{c-1} > MUT_i) \\ +RT_i^{c-1}, & \text{otherwise} \end{cases} \quad (13)$$

If $T_i^{c-1} > 0$, indicates cycle 'c' is negative and it represents an OFF status of i^{th} unit.

$$T_i^c = \begin{cases} -rand(MDT_i, RT_i^{c-1}), & \text{if } (RT_i^{c-1} > MDT_i) \\ -RT_i^{c-1}, & \text{otherwise} \end{cases} \quad (14)$$

Where, RT_i^{c-1} indicates the remaining scheduling period after allocating the first (c-1) cycles.

$$RT_i^{c-1} = T - \sum_{p=1}^{c-1} |T_i^p| \quad (15)$$

Formation of last cycle (T_i^C)

The duration of last cycle ‘C’ is decided by the duration of C-1 prior cycles (i.e) $T_i^C = RT_i^{C-1}$. If due to random generation of cycle duration the entire scheduling interval (T) is completed within the first few cycles ‘c’ < C then the remaining c+1..... C cycles are assigned to Zero. From this type of representation it is well known that the minimum up / down time constraint is satisfied in the coding stage itself and hence there is no need for any penalty function for this constraint in the objective function.

Leaping of worst solution

After formation of memplex, the local search process is carried out in each memplex. Leaping of worst frog towards the best frog is done by the random vector $D_i = rand(1) * (X_b - X_w)$ or by $D_i = rand(1) * (X_g - X_w)$. Addition of this vector to the X_w may lead to change in X_w and it needs the following modifications.

i) Now, the sum of all T_i^c of unit ‘i’ will not be equal to ‘T’. To adjust the following correction is done.

$$(T_i^1, T_i^2, \dots, T_i^C) = \frac{T * (T_i^1, T_i^2, \dots, T_i^C)_{i=1,2,\dots,N}}{\sum_{k=1}^C |T_i^k|} \quad (16)$$

(ii) The rand (1) function generates a random number between 0 and 1 the parameter which is a non-integer number and this may lead the parameter of X_w to a non-integer values. But X_w should be an integer vector. Hence to convert the non integer parameters of X_w to integer the following correction is done by

$$X_w^1 = \text{Round}(X_w) \quad (17)$$

(iii) The above round of correction may again lead to the sum not equal to ‘T’ Hence to adjust the values of T_i^c , the last non-zero cycle is adjusted as follows,

$$T_i^l = T - \sum_{k=1}^{l-1} |T_i^k|, i = 1, 2, \dots, N \quad (18)$$

(iv) After generation of new X_w , the minimum up / down time should be adjusted so that there is no violation in this constraint.

The correction in ‘c’ cycle should be followed by correction in ‘c+1’ cycle for adjusting the sum of T_i^c to ‘T’

For $T_i^1 > 0$ if $T_i^1 < \max(0, MUT_i - T_i^0)$, then the duration of cycle 1 & cycle 2 of unit ‘i’ are changed as

$$\begin{cases} T_i^2 = T_i^2 - T_i^1 + \max(0, MUT_i - T_i^0) \\ T_i^1 = \max(0, MUT_i - T_i^0) \end{cases} \quad (19)$$

For $T_i^1 < 0$ if $-T_i^1 < \max(0, MDT_i + T_i^0)$, then the duration of cycle 1 & cycle 2 of unit ‘i’ are changed

$$\begin{cases} T_i^2 = T_i^2 - T_i^1 + \max(0, MDT_i + T_i^0) \\ T_i^1 = -\max(0, MDT_i + T_i^0) \end{cases} \quad (20)$$

For $T_i^c > 0$ if $T_i^c < MUT_i$ for $c=2, \dots, C-1$

the cycles ‘c’ and c+1 of unit ‘i’ are changed

$$\begin{cases} T_i^{c+1} = T_i^{c+1} - T_i^c + MUT_i \\ T_i^c = MUT_i \end{cases} \quad (21)$$

For $T_i^c < 0$ if $-T_i^c < MDT_i$ for $c=2, \dots, C-1$ the cycles ‘c’ and c+1 of unit ‘i’ are changed

$$\begin{cases} T_i^{c+1} = T_i^{c+1} - T_i^c - MDT_i \\ T_i^c = MDT_i \end{cases} \quad (22)$$

After all the above corrections are carried out, on X_w , the Economic Dispatch (ED) should be carried out for each hour of scheduling horizon for all committed units. Then the fitness value is calculated. The sample frog is given in table:1

Computation of fitness function

The objective function of UC using SFLA has two terms, and they are the total operation cost and the penalty functions for violating system constraints (spinning reserve & power balance).

$$TC = \sum_{t=1}^T \sum_{i=1}^N FC_i (P_i^t) * X_i(t) + SU_T + SD_T \quad (23)$$

The penalty function has two terms. The first term for spinning reserve violation and is given by

$$\Pi_{res} = \omega \sum_{t=1}^T \frac{1}{D^t} R((D^t + R^t) - \sum_{i=1}^N X_i(t)P_{imax}^t) \quad (24)$$

the second term for excessive capacity is given by

$$\Pi_{cap} = \omega \sum_{t=1}^T \frac{1}{D^t} R(\sum_{i=1}^N X_i(t)P_{imin}^t - D^t) \quad (25)$$

where ‘ ω ’ depends on maximum operating cost of the system over a scheduling period ‘ T ’

$$\omega = \alpha T \sum_{i=1}^N FC_i(P_{imax}), \text{ where } \alpha \text{ is a constant.} \quad (26)$$

Now the objective is to minimize the fitness function

$$\text{Fitness} = A/(TC + \Pi_{res} + \Pi_{cap}) \quad (27)$$

$A = 10^8$. A is a system dependent constant added for avoiding the fitness value from obtaining too small values. This should be of the order of the system maximum operating cost.

TABLE:1 SAMPLE FROG FOR A 10 UNIT 5 CYCLE SYSTEM

Unit	1	2	3	4	5
	T_1^1	T_1^2	T_1^3	T_1^4	T_1^5
1	24	0	0	0	0
	T_2^1	T_2^2	T_2^3	T_2^4	T_2^5
2	24	0	0	0	0
	T_3^1	T_3^2	T_3^3	T_3^4	T_3^5
3	-4	19	-1	0	0
	T_4^1	T_4^2	T_4^3	T_4^4	T_4^5
4	-5	17	-2	0	0
	T_5^1	T_5^2	T_5^3	T_5^4	T_5^5
5	15	-9	0	0	0
	T_6^1	T_6^2	T_6^3	T_6^4	T_6^5
6	-8	6	-4	3	-3
	T_7^1	T_7^2	T_7^3	T_7^4	T_7^5
7	-8	6	-5	3	-2
	T_8^1	T_8^2	T_8^3	T_8^4	T_8^5
8	-9	4	-6	1	-4
	T_9^1	T_9^2	T_9^3	T_9^4	T_9^5
9	-10	2	-12	0	0
	T_{10}^1	T_{10}^2	T_{10}^3	T_{10}^4	T_{10}^5
10	-11	1	-12	0	0

V. SIMULATION RESULTS

The performance of SFLA to UC has been tested for various test systems such as IEEE 14bus(5 units), IEEE 30bus(6 units), IEEE 56bus(7 units), IEEE 118bus(19 units), a standard a 10 & 20 unit systems for a one day scheduling .The generator and load data are given in appendix A & B. The 10 unit system data is duplicated to obtain the 20 unit system data whereas the load data of 10 unit system is doubled for 20 unit system. The spinning reserve is assumed to be 10% of the load demand at each hour. The main parameters of SFLA have been taken from paper [17]. SFLA[12]has an initial population of 200 frogs and a set of 20 memplexes number of local search iteration is taken as 10.The SFLA program is developed and in MATLAB 2011’.

TABLE 2
UNIT COMMITMENT SCHEDULE OF 14 BUS SYSTEM (5 UNITS) FOR 24 HRS

Unit Hour	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
3	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
4	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	0	0	0
5	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0

TABLE 3
UNIT COMMITMENT SCHEDULE OF 30 BUS SYSTEM (6 UNITS) FOR 24 HRS

Unit Hour	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
3	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0
4	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0
5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	0
6	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	1

TABLE 4
UNIT COMMITMENT SCHEDULE OF 56 BUS SYSTEM (7UNITS) FOR 24 HRS

Unit Hour	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
3	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	1	1	1	1	0	0
4	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0
5	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
7	1	1	1	1	1	1	1	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	0	0

TABLE 5
UNIT COMMITMENT SCHEDULE OF 118 BUS SYSTEM (19UNITS) FOR 24 HRS

Unit Hour	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
3	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
4	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
5	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
6	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	0	0	1	1	0	0	0
7	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	0	0	0	1	1	1
8	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	0	0	0	0	1	1	1	1
9	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	1
10	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	1	1
11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
12	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
13	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
14	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
15	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
16	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1
17	0	0	0	0	0	0	0	0	1	1	1	1	1	1	0	0	0	0	0	0	1	1	1	0
18	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	0	0	1
19	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	1

TABLE 6
UNIT COMMITMENT SCHEDULE OF 10UNIT SYSTEM FOR 24 HRS

Unit Hour	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
3	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
4	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
5	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	1	1	0	0	0	0
6	0	0	0	0	0	0	0	0	1	1	1	1	1	1	0	0	0	1	1	1	1	0	0	0
7	0	0	0	0	0	0	0	0	0	1	1	1	1	1	0	0	0	0	0	1	1	1	0	0
8	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	0	0	1	0	0	0	0
9	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0

TABLE 7
UNIT COMMITMENT SCHEDULE OF 20 UNIT SYSTEM FOR 24 HRS

Unit Hour	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
3	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
4	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
5	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0	0	1	1	1	1	1	1	0	0	0	0	1	1	1	0	0	0
7	0	0	0	0	0	0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	0	0
8	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	0	0	1	1	0	0	0
9	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	1	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	1	0	0	0	0
11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
12	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
13	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
14	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0
15	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0
16	0	0	0	0	0	0	0	0	1	1	1	1	1	1	0	0	0	0	1	1	1	0	0	0
17	0	0	0	0	0	0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	0	0
18	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	0	0	1	0	0	0	0
19	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0
20	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0

TABLE 8
GENERATOR SCHEDULE OF 14 BUS SYSTEM (5 UNITS) FOR 24 HRS

Hour	Power Generations of Units(MW)				
	1	2	3	4	5
1	96.4	26.6	15.0	0	10.0
2	117.8	30.2	15	0	10.0
3	156.7	37.0	16.3	0	10.0
4	176.6	40.2	17.2	0	10.0
5	189.0	42.2	17.8	0	10.0
6	179.9	40.7	17.4	0	10.0
7	162.5	37.9	16.6	0	10.0
8	141.9	34.5	15.6	0	10.0
9	120.3	30.7	15.0	0	10.0
10	84.5	24.5	15.0	0	10.0
11	55.0	20.0	15.0	0	10.0
12	81.1	23.9	15.0	0	10.0
13	104.1	27.9	15.0	0	10.0
14	103.5	29.5	15.0	10.0	10.0
15	126.2	33.5	15.3	10.0	10.0
16	150.8	37.6	16.6	10.0	10.0
17	166.6	40.2	17.2	10.0	10.0
18	164.1	39.8	17.1	10.0	10.0
19	155.0	38.3	16.7	10.0	10.0
20	138.4	30.6	16.0	10.0	10.0
21	120.3	30.7	15.0	0	0
22	114.1	27.9	15.0	0	0
23	110.9	27.1	0	0	0
24	103.0	0	0	0	0

TABLE 9
GENERATOR SCHEDULE OF 30 BUS SYSTEM (6 UNITS) FOR 24 HRS

Hour	Power Generations of Units(MW)					
	1	2	3	4	5	6
1	95.3	33.7	15.0	10.0	0	12.0
2	119.0	38.6	16.4	10.0	0	12.0
3	145.7	43.5	17.8	10.0	0	12.0
4	177.9	48.0	19.1	10.0	0	12.0
5	190.0	49.9	19.6	11.9	0	12.0
6	182.2	48.6	19.2	10.0	0	12.0
7	160.0	45.6	18.4	10.0	0	12.0
8	132.8	41.1	17.1	10.0	0	12.0
9	115.8	38.0	16.2	10.0	0	12.0
10	91.1	32.9	15.0	10.0	0	12.0
11	79.5	30.5	15.0	10.0	0	12.0
12	90.3	32.7	15.0	10.0	0	12.0
13	98.4	34.4	15.2	10.0	0	12.0
14	110.2	36.9	15.9	10.0	0	12.0
15	128.7	40.4	16.9	10.0	0	12.0
16	148.1	44.0	17.9	10.0	0	12.0
17	159.9	45.7	18.4	10.0	0	12.0
18	167.4	45.3	18.3	0	10.0	0
19	163.3	44.6	18.1	0	10.0	0
20	154.4	42.9	17.6	0	10.0	0
21	137.5	39.8	16.7	0	10.0	0
22	133.1	38.9	0	0	10.0	0
23	151.0	0	0	0	10.0	0
24	119.0	0	0	0	0	12.0

TABLE 10
GENERATOR SCHEDULE OF 56 BUS SYSTEM (7 UNITS) FOR 24 HRS

Unit							
Hour	1	2	3	4	5	6	7
1	234.9	0	20.0	10.0	230.5	0	44.6
2	264.9	0	20.0	10.0	259.2	0	65.9
3	576.0	0	20.0	10.0	318.0	0	30.0
4	576.0	0	20.0	10.0	390.0	0	30.0
5	576.0	0	20.0	10.0	366.0	0	30.0
6	576.0	0	20.0	10.0	356.0	0	30.0
7	409.2	0	20.0	0	387.4	0	161.4
8	400.9	0	20.0	0	379.5	0	155.6
9	395.7	0	20.0	0	374.5	0	151.8
10	388.2	0	20.0	0	367.3	0	146.5
11	576.0	0	20.0	0	306.0	0	0
12	375.7	0	20.0	0	355.4	0	0
13	344.5	0	0	0	306.5	0	0
14	282.9	0	0	0	247.7	0	57.4
15	288.2	0	0	0	252.7	0	61.1
16	350.4	0	0	0	312.2	0	105.4
17	380.9	0	0	10.0	350.8	0	134.3
18	376.1	0	0	10.0	346.2	0	130.7
19	546.0	0	20.0	10.0	225.9	0	41.1
20	362.0	0	20.0	10.0	0	0	410.0
21	576.0	0	20.0	0	0	0	10.0
22	295.7	0	20.0	0	288.5	10.0	87.8
23	355.5	10.0	0	0	326.5	0	0
24	331.4	10.0	0	0	303.6	0	0

Solution of Unit Commitment Problem Using Shuffled Frog Leaping Algorithm

TABLE 11
GENERATOR SCHEDULE OF 118 BUS SYSTEM (19 UNITS) FOR 24 HRS

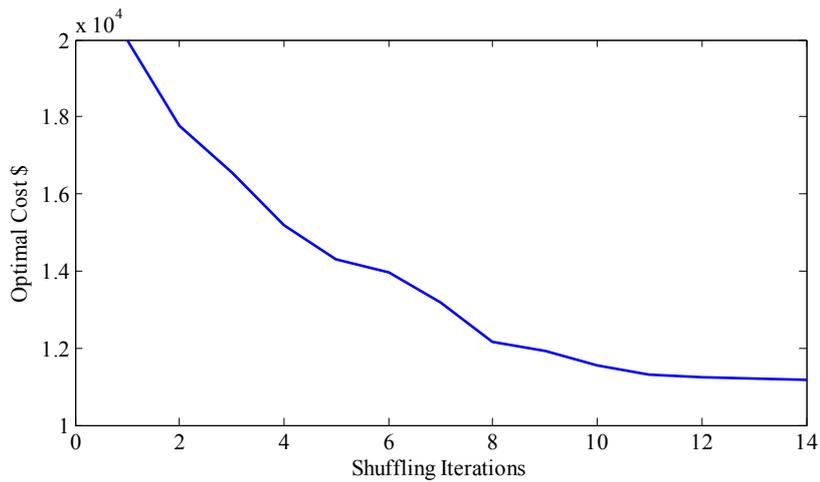
Unit	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Hour																			
1	367.2	10.0	30.0	163.0	1.0	0	0	0	0	0	290.1	291.3	900.0	430.7	0	681.7	0	5.0	0
2	372.9	10.0	30.0	167.3	1.0	0	0	0	0	0	295.3	296.5	900.0	436.80	0	685.0	0	5.0	0
3	500.0	10.0	30.0	151.4	1.0	0	0	0	0	0	282.2	283.4	900.0	421.4	0	665.6	0	5.0	0
4	500.0	10.0	30.0	77.7	1.0	0	0	0	0	0	400.0	400.0	900.0	317.3	0	659.0	0	5.0	0
5	500.0	10.0	30.0	143.8	1.0	0	0	0	0	0	400.0	400.0	900.0	410.6	1.0	659.6	0	5.0	0
6	500.0	10.0	30.0	134.0	1.0	0	0	0	0	0	400.0	400.0	900.0	600.0	1.0	659.0	0	5.0	0
7	500.0	10.0	30.0	163.4	1.0	0	0	0	0	0	400.0	400.0	900.0	600.0	1.0	675.6	0	5.0	0
8	500.0	10.0	30.0	110.3	1.0	0	0	0	0	0	400.0	400.0	900.0	593.7	1.0	659.0	30.0	5.0	0
9	486.0	10.0	30.0	40.0	1.0	3.0	0	0	0	0	400.0	400.0	900.0	600.0	1.0	659.0	30.0	0	0
10	500.0	10.0	30.0	40.0	1.0	3.0	30.0	5.0	0	0	400.0	400.0	900.0	600.0	1.0	490.0	30.0	0	0
11	454.0	10.0	30.0	40.0	1.0	3.0	30.0	5.0	0	20.0	400.0	400.0	900.0	288.1	1.0	638.0	30.0	0	0
12	404.0	10.0	30.0	40.0	1.0	3.0	30.0	5.0	20.0	20.0	400.0	400.0	900.0	258.8	1.0	647.2	30.0	0	0
13	500.0	10.0	30.0	40.0	1.0	3.0	30.0	5.0	20.0	0	400.0	400.0	826.9	244.1	1.0	634.0	30.0	0	0
14	500.0	10.0	30.0	40.0	1.0	3.0	30.0	5.0	20.0	0	400.0	400.0	900.0	600.0	1.0	235.0	30.0	5.0	0
15	500.0	10.0	30.0	40.0	1.0	3.0	30.0	5.0	20.0	0	400.0	400.0	900.0	600.0	1.0	471.0	0	5.0	0
16	500.0	10.0	30.0	72.0	1.0	3.0	30.0	5.0	0	0	400.0	400.0	900.0	600.0	1.0	659.0	0	5.0	0
17	500.0	10.0	30.0	81.0	1.0	3.0	30.0	0	0	0	400.0	400.0	900.0	600.0	1.0	659.0	0	5.0	0
18	500.0	10.0	30.0	184.6	1.0	0	30.0	0	0	0	400.0	400.0	872.6	462.6	1.0	688.2	0	5.0	0
19	500.0	10.0	30.0	147.8	1.0	0	0	0	0	0	400.0	400.0	900.0	410.6	1.0	659.6	0	0	0
20	185.0	10.0	30.0	40.0	1.0	3.0	0	0	0	0	400.0	400.0	900.0	600.0	1.0	700.0	0	0	0
21	500.0	10.0	42.2	228.2	1.0	3.0	0	5.0	0	0	400.0	400.0	900.0	600.0	1.0	0.0	119.6	0	0
22	500.0	10.0	30.0	201.3	1.0	0	30.0	5.0	0	0	400.0	400.0	894.3	584.0	1.0	0	96.4	0	0
23	302.5	10.0	30.0	152.0	0	0	30.0	5.0	0	20.0	276.9	278.1	900.0	415.2	1.0	673.1	54.2	0	0
24	500.0	10.0	30.0	176.1	1.0	0	30.0	5.0	20.0	20.0	400.0	400.0	878.2	0	0	686.7	0	5.0	4.0

TABLE 12
GENERATOR SCHEDULE OF 10 UNIT SYSTEM FOR 24 HRS

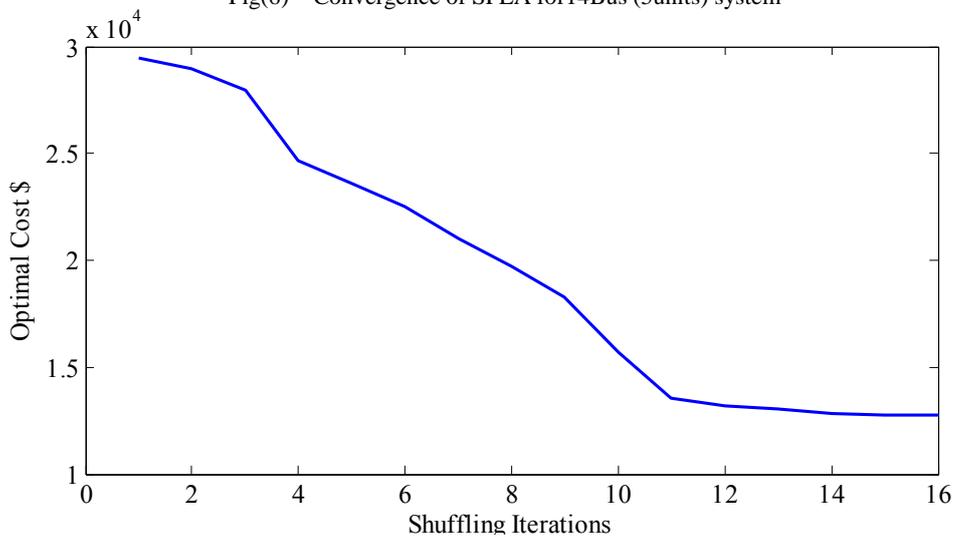
Hour	Power Generations of Units(MW)									
	1	2	3	4	5	6	7	8	9	10
1	455	220	0	0	25	0	0	0	0	0
2	455	270	0	0	25	0	0	0	0	0
3	455	370	0	0	25	0	0	0	0	0
4	455	455	0	0	40	0	0	0	0	0
5	455	390	130	0	25	0	0	0	0	0
6	455	360	130	130	25	0	0	0	0	0
7	455	410	130	130	25	0	0	0	0	0
8	455	455	130	130	30	0	0	0	0	0
9	455	455	130	130	85	20	25	0	0	0
10	455	455	130	130	162	33	25	10	0	0
11	455	455	130	130	162	80	25	10	10	0
12	455	455	130	130	162	80	58	10	10	10
13	455	455	130	130	162	33	25	10	0	0
14	455	455	130	130	85	20	25	0	0	0
15	455	455	130	130	25	0	0	0	0	0
16	455	335	130	130	0	0	0	0	0	0
17	455	285	130	130	0	0	0	0	0	0
18	455	365	130	130	0	20	0	0	0	0
19	440	455	130	130	25	20	0	0	0	0
20	455	455	130	130	162	33	25	10	0	0
21	455	455	130	130	85	20	25	0	0	0
22	455	455	130	35	0	0	25	0	0	0
23	455	315	130	0	0	0	0	0	0	0
24	455	345	0	0	0	0	0	0	0	0

TABLE 13
GENERATOR SCHEDULE OF 20 UNIT SYSTEM FOR 24 HRS

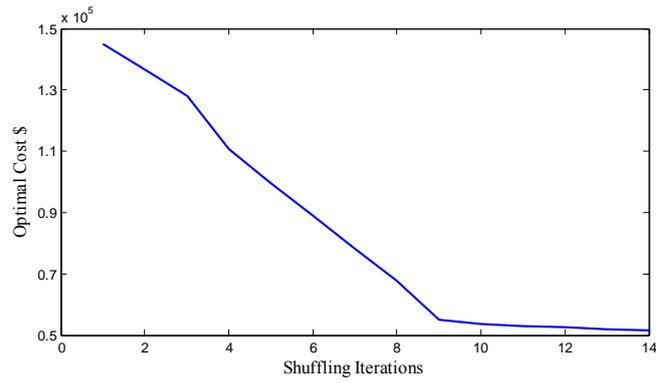
Hour	Power Generations of Units(MW)																			
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1	455	455	0	0	25	0	0	0	0	0	290	150	0	0	25	0	0	0	0	0
2	455	455	0	0	25	0	0	0	0	0	390	150	0	0	25	0	0	0	0	0
3	455	345	0	0	25	0	0	0	0	0	455	395	0	0	25	0	0	0	0	0
4	455	455	0	0	40	0	0	0	0	0	455	455	0	0	25	0	0	0	0	0
5	455	455	130	0	55	0	0	0	0	0	455	455	0	0	25	0	0	0	0	0
6	455	400	130	130	25	0	0	0	0	0	455	450	130	0	25	0	0	0	0	0
7	455	455	130	130	162	0	0	0	0	0	455	228	130	130	25	0	0	0	0	0
8	455	455	130	130	35	0	0	0	0	0	455	455	130	130	25	0	0	0	0	0
9	378	455	130	130	162	80	25	0	0	0	455	455	130	130	25	20	25	0	0	0
10	453	455	130	130	162	80	85	55	0	0	455	455	130	130	25	20	25	10	0	0
11	455	455	130	130	162	80	85	55	10	0	455	455	130	130	103	20	25	10	10	0
12	455	455	130	130	162	80	85	55	55	55	455	455	130	130	93	20	25	10	10	10
13	453	455	130	130	162	80	85	55	0	0	455	455	130	130	25	20	25	10	0	0
14	378	455	130	130	162	80	25	0	0	0	455	455	130	130	25	20	25	0	0	0
15	455	455	130	130	35	0	0	0	0	0	455	455	130	130	25	0	0	0	0	0
16	455	455	130	130	0	0	0	0	0	0	455	215	130	130	0	0	0	0	0	0
17	455	455	130	130	0	0	0	0	0	0	455	150	130	95	0	0	0	0	0	0
18	455	455	130	130	0	80	0	0	0	0	455	215	130	130	0	20	0	0	0	0
19	450	455	130	130	25	20	0	0	0	0	455	455	130	130	0	20	0	0	0	0
20	401	455	130	130	162	80	25	10	10	10	455	455	130	130	162	20	25	10	0	0
21	393	455	130	130	162	80	25	10	0	0	455	455	130	130	0	20	25	0	0	0
22	265	455	130	130	0	0	25	0	0	0	455	455	130	130	0	0	25	0	0	0
23	455	455	130	0	0	0	0	0	0	0	455	175	130	0	0	0	0	0	0	0
24	455	455	0	0	0	0	0	0	0	0	455	235	0	0	0	0	0	0	0	0



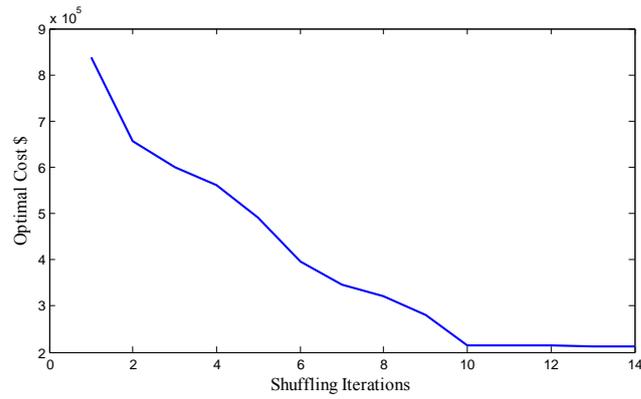
Fig(6) Convergence of SFLA for 14Bus (5units) system



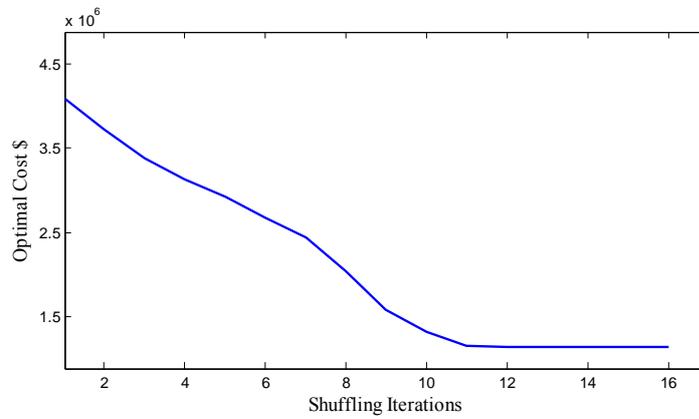
Fig(7) Convergence of SFLA for 30 Bus (6 units) system



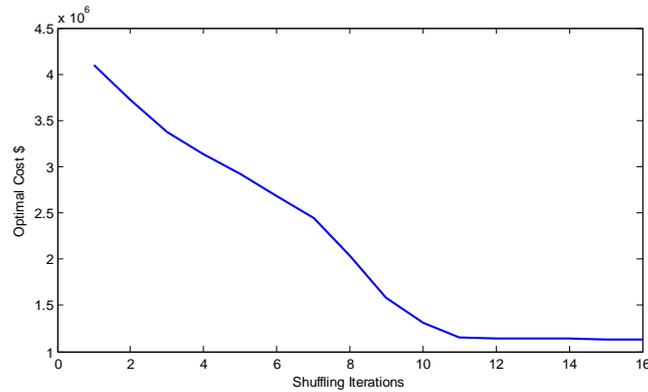
Fig(8) Convergence of SFLA for 56Bus (7 units) system



Fig(9) Convergence of SFLA for 118Bus (19 units) system



Fig(10) Convergence of SFLA for 10 Unit System



Fig(11) Convergence of SFLA for 20 Unit System

TABLE 14
OPTIMAL COST OF BEST RESULT OBTAINED USING SFLA

Sl.No	System	No.of generating Units	Optimal Cost(\$) SFLA
1	IEEE14BUS	5	11171
2	IEEE30BUS	6	12768
3	IEEE56BUS	7	51645
4	IEEE118BUS	19	211810
5	10 UNIT	10	564769
6	20 UNIT	20	1135800

TABLE 15
NO., OF SHUFFLING ITERATIONS TAKEN TO OBTAIN THE BEST RESULT USING SFLA

Sl.No	System	No.of generating Units	No., of Shuffling iterations
1	IEEE14BUS	5	12
2	IEEE30BUS	6	16
3	IEEE56BUS	7	14
4	IEEE118BUS	19	14
5	10 UNIT	10	16
6	20 UNIT	20	16

TABLE 16
COMPARISON OF OPERATION COST OF VARIOUS METHODS

No. of Units	Operational Cost (\$)		
	LRGA	IGCA	SFLA
10	565825	566404	564769
20	1130660	1124892	1135800

The commitment schedule of generators for various IEEE systems such as 14Bus (5 Units), 30Bus (6 Units), 56Bus (7 Units), 118 bus (19 Units), 10 Unit system, 20 Units system are tabulated in Table 2 to 7. The results of generation scheduling along with their real power generation of the best solution for 14Bus (5 Units), 30Bus (6 Units), 56Bus (7 Units), 118Bus(19 Units), 10 Unit system, 20 Units system are tabulated in Table 8 to 13. Table 14 gives the optimal cost of the best result obtained after several trials for all test systems. Table 15 gives the no., of shuffling iterations taken to obtain the best result. The optimal solution for all test systems is obtained between 12 to 16 shuffling iterations. The results of SFLA for 10, 20 unit systems are compared with the results of LRGA [7], ICGA [10] and is listed in Table 16. It is obvious that SFLA has satisfactory results in comparison with other methods. Fig. 6 to 11 shows the convergence rate of SFLA for the various systems considered in this work.

VI. CONCLUSION

In this paper, we presented a new evolutionary algorithm known as SFLA for UC problem. The integer coding is used to code the parameters of UCP. This type of coding directly satisfies the min up/down time constraints, and no need for any penalty function for this constraint. The performance of the proposed algorithm is tested for a one day scheduling and the results compared with LR & ICGA method. The simulation results show that the production cost of SFLA is less than the other methods such as LR & ICGA.

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APPENDIX: A

Load Data for all test systems

Hour	System	1	2	3	4	5	6	7	8	9	10	11	12
Load (MW)	14Bus	148	173	220	244	259	248	227	202	176	134	100	130
	30Bus	166	196	229	267	283.4	272	246	213	192	161	147	160
	56Bus	540	620	954	1026	1002	992	978	956	942	922	902	751
	75Bus	3352	3384	3437	3489	3659	3849	3898	3849	3764	3637	3437	3384
	118Bus	3170	3200	3250	3300	3460	3640	3686	3640	3560	3440	3250	3200
	10 Unit	700	750	850	950	1000	1100	1150	1200	1300	1400	1450	1500
Hour	System	13	14	15	16	17	18	19	20	21	22	23	24
Load(MW)	14Bus	157	168	195	225	244	241	230	210	176	157	138	103
	30Bus	170	185	208	232	246	241	236	225	204	182	161	131
	56Bus	651	588	602	768	876	863	843	802	784	702	692	645
	75Bus	3357	3394	3616	3828	3828	3786	3659	3458	3394	3334	3329	3348
	118Bus	3175	3210	3420	3620	3620	3580	3460	3270	3210	3153	3148	3166
	10 Unit	1400	1300	1200	1050	1000	1100	1200	1400	1300	1100	900	800

APPENDIX: B

14 BUS (5 UNIT) SYSTEM DATA

	Pmax	Pmin	A	B	C	MUi	MDi	Hcost	Ccost	Chour	IniState
Unit1	250	10	0.00315	2.0	0	1	1	70	176	2	1
Unit2	140	20	0.01750	1.75	0	2	1	74	187	2	-3
Unit3	100	15	0.06250	1.0	0	1	1	50	113	1	-2
Unit4	120	10	0.00834	3.25	0	2	2	110	267	1	-3
Unit5	45	10	0.0250	3.0	0	1	1	72	180	1	-2

30 BUS (6 UNIT) SYSTEM DATA

	Pmax	Pmin	A	B	C	MUi	MDi	Hcost	Ccost	Chour	IniState
Unit1	200	50	0.00375	2.0	0	1	1	70	176	2	1
Unit2	80	20	0.01750	1.70	0	2	2	74	187	1	-3
Unit3	50	15	0.06250	1.0	0	1	1	50	113	1	-2
Unit4	35	10	0.00834	3.25	0	1	2	110	267	1	-3
Unit5	30	10	0.0250	3.0	0	2	1	72	180	1	-2
Unit6	40	12	0.0250	3.0	0	1	1	40	113	1	-2

56 BUS (7 UNIT) SYSTEM DATA

	Pmax	Pmin	A	B	C	MUi	MDi	Hcost	Ccost	Chour	IniState
Unit1	576	50	0.001736	1.73647	0	3	2	70	176	3	4
Unit2	100	10	0.01000	10.0000	0	2	1	74	187	2	5
Unit3	140	20	0.007143	7.14286	0	3	1	50	113	3	5
Unit4	100	10	0.01000	10.0000	0	4	2	110	267	1	7
Unit5	550	40	0.001818	1.81818	0	1	1	72	180	1	5
Unit6	100	10	0.01000	10.0000	0	1	3	40	113	1	3
Unit7	410	30	0.002439	2.43902	0	2	1	70	176	2	4

118 BUS (19 UNIT) SYSTEM DATA

	Pmax	Pmin	A	B	C	MUi	MDi	Hcost	Ccost	Chour	IniState
Unit1	500	50	0.0018	1.818	0	3	2	70	176	3	4
Unit2	90	10	0.0054	5.405	0	3	1	74	187	2	-5
Unit3	300	30	0.0031	3.125	0	3	2	50	113	3	-5
Unit4	400	40	0.0024	2.415	0	4	2	110	267	1	7
Unit5	10	1	0.0093	9.346	0	1	1	72	180	1	-5
Unit6	23	3	0.0084	8.403	0	1	1	40	113	1	-3
Unit7	240	30	0.0033	3.289	0	2	1	70	176	2	-4
Unit8	50	5	0.0068	6.757	0	3	1	74	187	1	-5
Unit9	200	20	0.0039	3.922	0	4	5	50	113	3	-5
Unit10	200	20	0.0038	3.846	0	2	1	110	267	1	-7
Unit11	400	90	0.0020	2.037	0	3	2	72	180	2	-5
Unit12	400	90	0.0020	2.032	0	3	1	40	113	1	-3
Unit13	900	100	0.0012	1.242	0	3	2	70	176	2	10
Unit14	600	50	0.0017	1.733	0	2	1	74	187	1	-5
Unit15	5	1	0.0096	9.615	0	1	1	50	113	0	-5
Unit16	700	50	0.0014	1.414	0	2	2	110	267	1	7
Unit17	300	30	0.0028	2.841	0	3	1	72	180	2	-5
Unit18	50	5	0.0071	7.143	0	3	1	40	113	1	-3
Unit19	40	4	0.0074	7.353	0	1	1	70	176	0	-4

10 UNIT SYSTEM DATA

	Pmax	Pmin	A	B	C	MUi	MDi	Hcost	Ccost	Chour	IniState
Unit1	455	150	0.00048	16.19	1000	8	8	4500	9000	5	8
Unit2	455	150	0.00031	17.26	970	8	8	5000	10000	5	8
Unit3	130	20	0.002	16.60	700	5	5	550	1100	4	-5
Unit4	130	20	0.00211	16.5	680	5	5	560	1120	4	-5
Unit5	162	25	0.00398	19.70	450	6	6	900	1800	4	-6
Unit6	80	20	0.00712	22.26	370	3	3	170	340	2	-3
Unit7	85	25	0.00079	27.74	480	3	3	260	520	2	-3
Unit8	55	10	0.00413	25.92	660	1	1	30	60	0	-1
Unit9	55	10	0.00222	27.27	665	1	1	30	60	0	-1
Unit10	55	10	0.00173	27.79	670	1	1	30	60	0	-1