Analysis and Design of Multi Cell Post-Tensioned PSC Box Girder

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Abstract: In the present work, analysis and design of box girder has been done, considering two different sheathing pipes namely HDPE and corrugated Bright metal pipes. These sheathing pipes have been used to find the economic solution of design of multi-cell box girder. CSI-bridge modular software has been used for carrying out analysis. Multi-cell PSC box girder design has been performed at various locations along the span so as to consider maximum or critical locations of the PSC box girder due to various loading conditions, the post tensioning of cables is done for jacking load at 0.765 times the UTS and jacking is done at both ends of the PSC box girder simultaneously., Various losses that occur due to different phenomena such as elastic shortening, Creep, shrinkage, friction and wobble loss have been considered. The results obtained on the two sheathing pipes are compared and are tabulated and graph gas been plotted. Encouraging results have been obtained.

Keywords: High density polyethylene (HDPE), Bright metal, Indian road congress (IRC), Pre-stressed concrete (PSC),

I. Introduction

A Bridge or flyover can be defined as a structure including supports erected over a gorge or an obstruction, such as water, highway, or railway, and having a track or passageway for carrying traffic or other moving loads. A box girder bridge is an apparent bridge sector in which main beams contain girders in the hollow box shape. The box girder usually includes either structural steel, pre-stressed concrete or in the form of reinforced concrete or composite section. It is typically trapezoidal, square or rectangular in cross-section. Box girder bridges are normally used for bridges, flyovers and at grade separators. Normally pre-stressed box girders are adopted for longer spans only (span range 30 to 90m) due to the fact that pre-stressed concrete box girder the depth of the box girder can be reduced drastically when compared to normal I-girders and the depth of the box girder again depends on the number of webs provided. As the number of web increases the depth of the box girder also reduces. Box girders a most suitable for spans in curved alignment due to their high torsional rigidity. In this present work, one such multi-cell box girder for a span of 35m has considered. Fig 1 shows a schematic representation of multi cell box girder.



Fig.1 longitudinal view of Multi cell box girder

II. Literature Review

C. Mortensen et., al.,(2003)¹presented the paper about the effect of creep, shrinkage Losses in Prestressed Concrete Bridges in highly changing Variable Climates in this study is also clarifies about the moist curing after the stressing is also causes in the reduction of the long term losses.

P. J. Barret., al.,(2005)²in their paper studied temperature variations effects on precast pre-stressed concrete girders bridges. During manufacturing time and during its service life of pre-stressed girder the effect temperature variations in the girder member can be seen and to calculate exact strains developed in the girders, using of curing with high temperatures during the girder fabrications may cause the thermal expansion in the pre-stressed girders due to the cable which is used for pre-stress is steel due to high temperature elongation of

cable will occur and loss of pre-stress may occur to overcome this problems using more quantity of steel and concrete quantity if increased in girders it may decreases simultaneously.

G. Venkata Siva Reddyet., al., (2014)³ presented the paper regarding the response of the box girder bridge based on the moving load analysis. Models and analysis has been carried out using FEM based software influence surfaces and influence lines are generalised to analyse the bridge structure subjected to moving loadings with in the lanes defined.Based on the obtained results some of the conclusions they have drawn that asfor multiple cell box girders are having good resistance in the performance of the box girder.

III. Methodology

A. Modelling

Modelling is carried out using CSI-Bridge 2015 (Structural Analysis Programming) software of version 17.2.0 this software is basicallyfinite element method software and Finite element method is the most versatile method, which can easily handle structures of complicated shapes, and boundary conditions. It involves subdivision of the whole structure into number of small elements. Before modelling all the parameters of box girder structure has to be decided based on the IRC standards. In modelling of box girder, main parameter is input of the sizes of box girder and its supporting property and after assigning section property parameter next step part is loading part where lane justification live load application and super imposed dead load application on box girder, different live load application is done to get worst case of live load. In this case, two 70R loading will govern the live loading, once all loading is done analysis proceeds as per standard practice. Fig 2 shows full view of box girder as a wire mesh model and fig 3 shows the four lane arrangement on the deck of box girder, fig 4 shows 70R vehicle loading arrangement on box girder.



Fig.2 Frame element of Multi cell box girder



Fig.3 Multi cell box girder with four lane arrangement



Fig.4 70R vehicle loading arrangement

B. Design

The design of PSC box girder is performed using self-developed spread sheets. The design is done as per IRC stipulations, the design procedure comprises of the following units.

- 1. Calculation of section properties
- 2. Tabulation of summary of bending moment and shear force
- 3. Calculation of stress developed due to bending moment and shear force
- 4. Cable profiling to suit the geometry
- 5. Calculation of loss of pre-stress due to friction, wobble effect and slip loss
- 6. Design of end block
- 7. Calculation of time dependent losses
- 8. Check for stresses in service and other cases
- 9. Calculation of temperature stresses
- 10. Stress check for permissible limit in service case as per IRC
- 11. Check for deflection
- 12. Check for ultimate strength
- 13. Check for ultimate shear strength

C. Salient Features Of The Pscbox Girder

- 1. Type of the structure is multi cell post tensioned PSC boxgirder
- 2. Length of box girder = 35.0m
- 3. Depth of box girder = 2.0m
- 4. Total top width of box girder = 16.6m
- 5. Total bottom width of box girder = 13.10m
- 6. Thickness of web = 0.325m (At running section)
- 7. Thickness of web = 0.600m (At end section)
- 8. Thickness of bottom slab = 0.325m (At running section)
- 9. Thickness of bottom slab = 0.750m (At end section)
- 10. Thickness of top slab = 0.275m
- 11. Effective width of top slab = 6.550m
- 12. End diaphragm thickness = 0.75m (2 no's)
- 13. Mid diaphragm thickness = 0.75m (2 no's)
- 14. Number of cells = 2no's
- 15. Grade of concrete = M45
- 16. Grade of steel = Fe500
- 17. Type of strands = 19T15 (main cable)
- 18. Type of strands = 19T15 (dummy cable)
- 19. Type of sheathing duct = HDPE/Bright Metal
- 20. Total number of cable used = 18 No's
- 21. Method of pre-stressing = Post tensioning

IV. Results And Discussions

A. Bendging Moment And Shear Force

Variation of bending moment and shear force in full span for different loading cases is shown in fig 5 and fig 6.For dead load the bending moment and shear force value will be more and minimum bending moment and shear force for median, the box girder is analysed as a simply supported and maximum moments will be at midspan and there will be negative moments at supports and maximum shear force at support and there will be minimum shear force at midspan.



Fig.5 Bending moment diagram for different loadings



Fig.6 Shear force diagram for different loadings

B. Displacement

Displacement is calculated at the centre of the span for different loading case where the maximum deflection will occur and is tabulated in table 1 and figure 7 shows the deformed shape of Box Girder for one of the loading case from fig 4 it can be observed that the deformation pattern on loading of box girder at centre of span the deformation will be more and it will be gradually decrease towards the support, the variations in deformation is shown with specific colours

Displacement for Different Loading Case									
Joint	OutputCase	CaseType	StepType	U1	U2	U3			
Text	Text	Text	Text	m	m	m			
2160	DEAD	LinStatic		-0.000245	0.000259	-0.024431			
2160	LIVE LOAD	LinMSStat	Max	0	0.00018	0			
2160	LIVE LOAD	LinMSStat	Min	-0.000086	0	-0.008316			
2160	CRASH BARIER	LinStatic		-0.000015	0.000054	-0.001975			
2160	WEARING COAT	LinStatic		-0.00002	0.00002	-0.001955			
2160	MEDIAN	LinStatic		-0.000004473	0.000003073	-0.000378			
2188	DEAD	LinStatic		-0.000245	-0.000259	-0.024431			
2188	LIVE LOAD	LinMSStat	Max	0	0.000024	0			
2188	LIVE LOAD	LinMSStat	Min	-0.000076	0	-0.006563			
2188	CRASH BARIER	LinStatic		-0.000015	-0.000054	-0.001975			
2188	WEARING COAT	LinStatic		-0.00002	-0.00002	-0.001955			
2188	MEDIAN	LinStatic		-0.000004473	-0.000003073	-0.000378			

 Table.1

 Displacement for Different Loading Case



Fig.7 Deformed Shape of Box Girder

C. Cable Profile

The variation of cable is shown in the fig 8 the arrangement of cable in y-direction and there will be parabolic curve for all set of cables as shown in the fig8 and in fig 9 it is shown that how cables are arranged in box girder at end section an in running section. In all 18no's of main cable are provided in three webs of the box girder and also on the bottom soffit slab of the box girder two emergency cable are provided in the outer web of the box girder, cables provided in the webs will be more effective than the cables provided in the bottom soffit slab.



Fig.9 Cable arrangement at End block and Running section

D. Elongation Of Cable

The total elongation variations in all cables due to pre-stressing is shown in fig 10. From the figure it is concluded that HDPE sheathing material have more elongation than the Bright Metal by this we can reduce the pre-stressing force in HDPE and one can achieve an economic design.



Fig.10 Total Elongation of Cables

E. Time Depandent Loses

The losses due to the time dependent factors such as elastic shortening, creep, shrinkage, relaxation are shown in fig 11 to 14, it is observed that the percentage of loss except due toshrinkage loss in box girder when two different material is used, HDPE will be more than bright metal but in shrinkage the loss in HDPE will be less when compared to bright metal, so by comparing these losses we can reduce the pre-stressing steel by which force reduction can be achieved and corresponding time dependent losses can be lowered and economic design of pre-stressed box girder can be achieved.



Fig.11 Elastic shortening loss Percentage



Fig.12 Creep loss Percentage



Fig.13 Shrinkage loss Percentage



Fig.14 Relaxation of steel loss Percentage

F. Force Vartion In Psc Box Girder

Force obtained in all cables are plotted for two different materials i.e., Bright metal and HDPE as shown in fig 15, jacking force applied at the end block portion of box girder is 3789KN and the force will be gradually decreasing until it reaches at the centre of the box girder span. In this present work, box girder is designed by considering both end pre-stressing, the force 3789KN is applied simultaneously from the both ends of the box girder at the same time during transferring of force in box girder some sudden losses will take place. Friction and wobble effect the values considered for friction and wobble in this work is for HDPE friction coefficient value is 0.17 and wobble coefficient value is 0.002 and for Bright metal friction coefficient value is 0.25 and wobble coefficient value is 0.0046 respectively. These values are recommended as per IRC standards and approximate slip is considered is about 6mm in the design for checking the force reduction in the pre-

stressing force. As obtained from results it is found that HDPE used design gives more force than the Bright metal material used design, we can achieve more force in pre-stressed box girder by using HDPE material and number of cables can also be reduced by using HDPE materials in pre-stressed box girder.



Fig.15 Force variation in cables due to Bright metal and HDPE

G. Stress Vartion In Psc Box Girder

The variation of stresses in PSC box girder is shown in fig 16 to 19, stress variations is taken after application of pre-stressing force in box girder. Stresses to due self weight of box girder, live load and prestressing force is combined to get final stress and these results are finally combined with the temperature rise and temperature fall loading cases. Resultantstress is found to be safe and well within the limit as per IRC stipulations. Stress developed for HDPE material used design the stress value at centre section of box girder at bottom for service and temperature rise case is of 1.594 N/mm² and top is 4.944 N/mm² and for service and temperature fall case at bottom is about 1.294 N/mm² and top is 5.909 N/mm². Stress developed for Bright metal material used design the stress value at centre section of box girder at bottom for service and temperature rise case is of 1.267 N/mm² and top is 4.959 N/mm² and for service and temperature fall case at bottom is 4.959 N/mm² and for service and temperature fall case at bottom is about 0.966 N/mm² and top is 5.924 N/mm². These values are shown in fig 16 to 19. From the result it is observed that HDPE will be more efficient compared to Bright metal in PSC box girders.



Fig.16 Stress variation at top of box girder due to service and temperature rise loading



Fig.17 Stress variation at bottom of box girder due to service and temperature rise loading



Fig.18 Stress variation at top of box girder due to service and temperature fall loading



Fig.19 Stress variation at bottom of box girder due to service and temperature fall loading

H. Check For Ultimate Strength At Various Cross Sections

Different section are considered for ultimate strength check of PSC box girder and it is found to be with in the limit, ultimate strength check is done as per IRC code standards and the ultimate moment is less than the crushing strength of concrete and yield stress of steel and is shown in table 2

M _{ultimate} 1.25 X DL + 2 X SIDL + 2.5 X LL	7.79E+09	3.31E+10	5.29E+10	7.61E+10	9.14E+10	9.71E+10
M _{ultimate} Crushing of Concrete(N- mm)	1.41E+11	1.54E+11	1.61E+11	1.69E+11	1.73E+11	1.75E+11
M _{ultimate} Yield of Steel (N-mm)	1.55E+13	1.68E+13	1.77E+13	1.85E+13	1.89E+13	1.90E+13
RESULT	SAFE	SAFE	SAFE	SAFE	SAFE	SAFE

Table 2: Ultimate strength at various section of box girder

V. Check For Ultimate Shear Strength At Various Sections

Ultimate shear strength of box girder at different sections is checked as per the IRC: 18 and the values obtained is found to be within in the limits and is shown in table 3 and table 4. Shear check is done both HDPE and Bright metal.In Ultimate shear strength, HDPE will give effective results than the Bright metal, the entire box girder is dived into different sections and for shear strength the box girder is found to be within limits for both cases but at centre of the span it will be a cracked section and these sections can be provided with some untension reinforcement.Resultant stress variations will be there in both the cases and HDPE gives better performances as per the design of present work and is shown in table 3 and 4.

Table 3: Ultimate shear strength ofbox girder at	t different section for HDPE
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M _{ult}	(N-mm)	7.79E+09	3.31E+10	5.29E+10	7.61E+10	9.14E+10	9.71E+10
V _{ult}	(N)	1.00E+07	8.38E+06	7.05E+06	5.31E+06	2.83E+06	3.21E+05
V _{cr(r}	nin) (N)	7.16E+05	7.16E+05	3.47E+05	3.47E+05	3.47E+05	3.47E+05
Vcr	(N)	6.17E+07	1.24E+07	6.50E+06	3.48E+06	1.63E+06	2.88E+05
RESULT		UNCRAC	UNCRAC	UNCRAC	UNCRAC	UNCRAC	CRACKE
		KED	KED	KED	KED	KED	D

M _{ult}	(N-mm)	7.79E+09	3.31E+10	5.29E+10	7.61E+10	9.14E+10	9.71E+10
V _{ult}	(N)	1.00E+07	8.38E+06	7.05E+06	5.31E+06	2.83E+06	3.21E+05
V _{cr(min)}	(N)	7.16E+05	7.16E+05	3.47E+05	3.47E+05	3.47E+05	3.47E+05
Vcr	(N)	5.91E+07	1.20E+07	6.31E+06	3.43E+06	1.59E+06	2.83E+05
RESULT		UNCRAC	UNCRAC	UNCRAC	UNCRAC	UNCRAC	CRACKE
KL	JULI	KED	KED	KED	KED	KED	D

Table 4: Ultimate shear strength of box girder at different section for Bright metal

J. Check For Deflection At Midspan

Deflection check is done for both the cases at centre of the span which is critical, the net downward deflection is 32.205mm and net upward deflection due to PSC for HDPE is 24.126mm and resultant will be 8.08mm downward which is within the limits as per IRC standards(L/500=68.5mm) and Bright metal it is about 23.378mm and resultant will be about 8.83mm downward which is within the limit of 68.55mm and it is observed that HDPE will give less deflection than the Bright metal and hence in this case, structural stability will be more effective.

VI. Conclusions

- 1. The design of PSC multi-cell box girder performed is found to be an economical design corresponding critical bending moment and shear forces developed due to various load combinations as per IRC specifications in comparison with the design of similar span configuration using I girders with Cast In Situ (C.I.S) deck slab.
- 2. Two types of sheathing pipes have been used for cable ducts of PSC box girder modelling. The first type being HDPE pipes whereas second type is of corrugated bright metal sheathing pipes. The results obtained in girder with HDPE pipes are found to be more viable than corrugated bright metal pipes since the loss of pre-stress is much less in case of HDPE pipes thereby increasing the stress levels in the concrete sections.
- 3. The cable profile has been determined so as to suit the bending moment diagram and cable profile adopted in the box girder is found to be most suitable considering the kern distances of the PSC section.
- 4. The stresses that are developed in the box girder at service condition is found to be well within the permissible limits as per IRC specifications and no tension being developed at any cross section in the girder at service condition.
- 5. Finite Element Analysis of Box Girder from CSI Bridge modeler software is found to be more accurate and close to reality in comparison to other analysis methods. The FEA results are in good agreement with the results obtained from other methods.
- 6. It is found that the deflection obtained due to various loading conditions and at service condition is well within permissible limits as per IRC. The maximum vertical deflection is found to occur near mid-span location of the girder.
- 7. The temperature stresses that are developed due to temperature gradient as per IRC have been checked and combined with the final stresses. The maximum final stresses are found to be in good agreement with the allowable values.
- 8. The design has also been checked for Ultimate moment and Ultimate shear cases separately as per IRC guidelines and the design is found to be safe in all respects.

References

- C. Mortensen, M. Saiidi, and S. Ladkany Creep and Shrinkage Losses in Prestressed Concrete Bridges in Highly Variable Climates- TRB 2003 Annual Meeting CD-ROM
- [2]. P. J. Barr, J. F. Stantonand M. O. Eberhard Effects of Temperature Variations on Precast Pre-stressed Concrete Bridge Girdersjournal of bridge engineering © asce / march/April 2005
- [3]. Venkata Siva Reddy, P. Chandan Kumar Response of box girder bridge spans-g. International Journal of Bridge Engineering (IJBE), Vol. 2, No. 2-2014
- [4]. Khaled M. Sennah and John B. Kennedy Literature Review in Analysis of Box-Girder Bridges- Journal of Bridge Engineering, Vol. 7, No. 2, March 1- 2002.
- [5]. Erin Hughs and Rolaldriss -Live-Load Distribution Factors for PrestressedConcrete,Spread Box-Girder Bridge-Journal of Bridge Engineering, Vol. 11, No. 5, September 1-2006
- [6]. Dr. Husain M. Husain and Mohanned I. Mohammed Hussein Finite element analysis of post-tensioned concrete box girders-Journal of Bridge Engineering (2007)
- [7]. Hiroshi Mutsuyoshi& Nguyen DucHai Recent technology of prestressed concrete bridges in Japan- IABSE-JSCE Joint Conference on Advances in Bridge Engineering-II, August 8-10-2010
- [8]. Ali FadhilNaser and Wang Zonglin-Finite Element and Experimental Analysis and Evaluation of Static and Dynamic Responses of Oblique Pre-stressed Concrete Box Girder Bridge- Research Journal of Applied Sciences, Engineering and Technology 6(19): 3642-3657- 2013
- [9]. T Y lin and A P burns, Design of Pre-stressed Concrete Structures, John Wiley & Sons, 3rd Edition edition, 12 August 1981
- [10]. N Krishna Raju, pre-stressed concrete, Tata McGraw-Hill Education, 01-Dec-2006
- [11]. DR. V. K. Raina, Concrete bridges hand book, Galgotia publications, first edition, 1999
- [12]. IRC:6-2000 standard specification and code of practice for road bridges
- [13]. IRC:18-2000 design criteria for pre-stressed concrete road bridges