

Reconfigurable Distributed Arithmetic Based Adaptive Noise Canceller Using Modified NLMS Algorithm

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Abstract: This paper presents an efficient design and implementation of low area, high speed Adaptive filter based on Distributed Arithmetic (DA) Scheme. An enhanced NLMS algorithm has been proposed for the adaptive noise cancellation filter design. The computation speed of the proposed NLMS system is relatively high due to preallocation of memory for variables in enhanced Normalized LMS algorithm. The proposed design is successfully implemented using Matlab Code and Xilinx ISE Design Suit on Spartan 3 based XC 35400 and Spartan 3E based Xc3500e FPGA device. The synthesis report shows a considerable decrease in device utilization percentage and increase in overall speed than the existing design. For 20 tap proposed filter there is 43% reduction in number of slices, 59% reduction in number of flip flops, 24% reduction in number of LUTs used, whereas 54% improvement has been achieved in maximum frequency and 35.14% improvement in minimum period. Whereas for 10 coefficient filter there is 21% increase in maximum frequency and 16.46% decrease in minimum period.

Keywords: Adaptive Filters, Distributed Arithmetic, FPGA, NLMS Algorithm, Noise Cancellation.

I. Introduction

In this era of extensive telecommunication systems, the efficient signal processing is one of the biggest challenges as the signals suffer interference and noise caused by various transmission mediums. To improve the quality of communication, an effective noise cancellation method is required [1]. Noise Cancellation refers to the process of optimal filtering that includes estimation of the noise by filtering the reference signal and deducting this estimated noise from the primary input which contains both signal and noise. In adaptive filtering process when an input signal containing noise is applied to the filter, a negative feedback is applied which depends on the noise in the input signal by adjusting weights values which cancels out the noise from input signal [2].

Over the past two decades, digital signal processors have been changed revolutionary to improve speed and efficiency of communication systems. Many advancements have been made in DSP over the past three decades in speed improvement, area and power consumption. The researchers have put a great effort in crafting efficient Digital Signal Processing (DSP) functions architecture such as FIR filters, which are most commonly used in various telecommunication applications. Adaptive filter is one of the effective solution to filter out noise less signals in a communication system. Adaptive filter changes filter coefficients with time to adapt to the dynamic input signal environment [3].

Fig. 1 represents a standard Adaptive Noise Cancellation process in which there are two inputs: one is primary signal and other is reference signal. The primary signal x_n is corrupted by the noise n_n added by means of communication mediums or external environment. The reference signal nr_n is second input which is similar to or correlated with the noise signal n_n . The reference noise passes through an Adaptive Filter to produce an output nf_n which nearly resembles noise n_n present in the primary input [4]. This estimated noise (nf_n) is subtracted from the primary input signal ($x_n + n_n$) to produce the estimated error e_n and output y_n which is similar to the signal x_n .

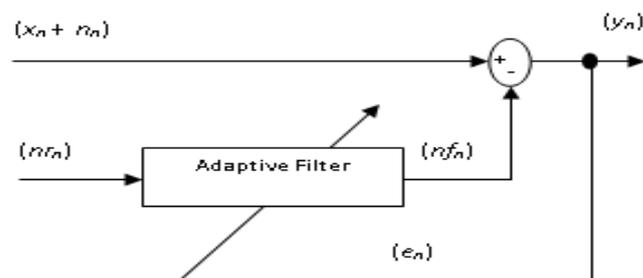


Fig. 1: Standard Adaptive Noise Canceller Organization

There has been a tendency to implement DSP functions in Field Programmable Gate Arrays (FPGAs) for last few years, which provides a balanced solution in terms of area and speed of communicating device in comparison with traditional devices [5]. FPGAs also offer an attractive solution that balances high flexibility and cost of a device. Previously, the design methods were mainly focused on multiplier based architectures also known as multiply and Accumulate (MAC) blocks constituted in several DSP functions. This requires an appreciable number of multipliers and hence a considerable amount of hardware. But now a days, the multiplier less Distributed Arithmetic (DA) based technique has been considered a very reliable approach due to its high throughput and regularity, due to which a cost effective and time efficient devices can be obtained [6].

II. Background Concepts

In this section DA based Adaptive Filters and Adaptive filtering algorithms are presented that are best suited for hardware implementation. DA algorithm becomes quiet fast, when the number of elements in a vector is same as the word size. The beauty of the technique is that the DA algorithm replaces the multiplications by ROM Look up tables [7]. This is an efficient way for implementing FPGAs.

2.1 Distributed Arithmetic

Distributed Arithmetic was first introduced by Croisier et al. and further developed by Peled and Lui [8]. It is based on a multiplier-less implementation of FIR filters through a bit-serial computation using all possible combination sums of the filter coefficients [9].

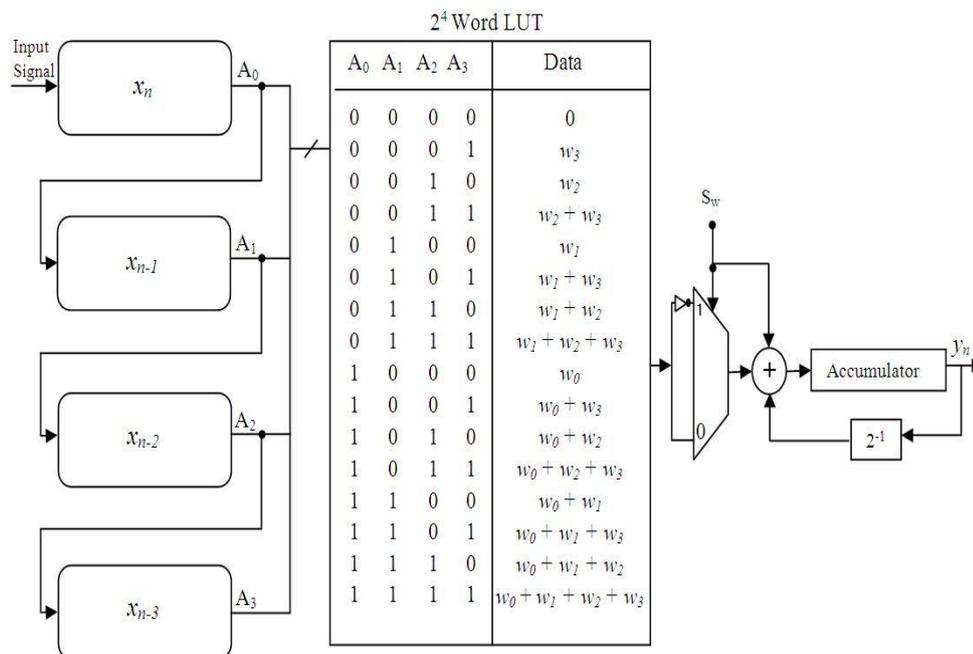


Fig. 2. Basic DA based FIR filter

Fig. 2 presents the Distributed Arithmetic (DA) implementation for four-tap FIR filter where x_n denotes samples of coming input signal. These samples are stored in the shift-registers in a manner that the latest sample is stored on the top most register and the oldest is stored in the last register [10]. Lookup Table (LUT) contains the partial product of Least Significant Bits (LSBs) taken from each of the shift registers for the address lines. The DA architecture is based on storing all the possible combinations of the coefficients w_n in lookup table [11].

2.2 Least Mean Square Algorithm

LMS algorithm was first proposed in year 1960 by Widrow and Holf. This algorithm is used to minimize Mean Square Error (MSE) by adjusting weight coefficients for each sample of coming input sample. Most of the noise cancellation applications use this algorithm. This algorithm can be understood in two phase: Filtering Phase & Weight Updation Phase [12]. In filtering phase unwanted signal is filtered by using close estimation of unwanted signal and initial weight coefficients. The output of this phase nearly resembles the desired signal. In weight updation phase, weight coefficients are updated on the basis of error feedback from the previous filtering phase [13]. The updated weight is now used for the next filtering process. Equation 1 represents the weight updation equation for LMS algorithm.

$$w_n = w_{n-1} + \mu e_n x_n \tag{1}$$

In the above equation w_n denotes updated weight coefficient and w_{n-1} denotes previous weight. Step size is denoted by μ , x_n is input signal sample and e_n is estimated error signal. For very small values of μ filter may become unstable due to more time of convergence. The output of adaptive process is given as per the equation below:

$$y_{n+1} = w_{n+1} * x_{n+1} \tag{2}$$

2.3 Normalized Least Mean Square Algorithm

Least Mean Square Algorithm has limitation that it may become unstable as signal power changes. To overcome this problem Normalized Least Mean Square (NLMS) algorithm was introduced. The instability in the LMS algorithm is caused by the very small values of Step Size (μ) [14]. But in case of NLMS the input power is normalized to impose very less effect on the weight updation process. The weight updation equation for NLMS algorithm is given as equation 4 in which C_n denotes the normalization constant which can be calculated as equation 3:

$$C_n = x_n^2 + .0001 \tag{3}$$

$$w_n = w_{n-1} + \mu / C_n * e_n * x_n \tag{4}$$

The normalized form of LMS algorithm provides more stability as well as high rate of convergence for the adaptive filtering process [15].

III. Proposed Design

In this section proposed methodology and design for DA based Adaptive Filter is presented, which uses enhanced NLMS algorithm. For this purpose traditional NLMS algorithm is replaced by proposed NLMS algorithm for adaptive filtering. In the proposed algorithm we have introduced concept of memory preallocation for variables which results in increased computational speed for the filtering system. The following pseudo code explains the proposed adaptive methodology. The notations used in the algorithm are described as under:

- x_n : Input Signal
- $h[p,n]$: Convolution Matrix generated using x_n
- Dn : Desired Output
- $w[p,n]$: Weight Matrix
- e_n : Estimated Error
- y_n : Filter Output
- μ : Step Size
- z : Impulse Response
- C_n : Normalization Constant

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h[p,n]= conv(x_n, z) /*Convolution Matrix of Input Signal x_n and Impulse response z */
C_n= h[n,:]*h[n,:]' + 0.0001 /*Determining Normalization Constant using convolution matrix*/
e_n = d_n - w[n,:] * h[n,:]' /*Error calculation*/
w[n,:] = w[n-1,:] + mu/C_n * e_n * conj(h[n,:]) /*Updating Weight Matrix*/
y_n = w[n,:] * h[n,:]' /*Filter Output Calculation*/
    
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The final output of the adaptive system is calculated by subtracting y_n from the input signal containing noise. We have implemented the proposed algorithm on FPGA using Distributed Arithmetic algorithm. Results of the simulation of algorithm and synthesis report of hardware implementation of the same is discussed in next section.

IV. Results And Discussion

The proposed algorithm of Normalized LMS algorithm is initially simulated using Matlab code and afterwards Distributed Arithmetic based implementation on a target FPGA of the same is done by converting M code to VHDL code. Design was exposed to variable step size and filter order to test the adaptability and stability of the proposed technique. To observe the behavior of proposed design, the input signal x_n with sampling frequency $f_s=48000$ Hz is taken. Initially we observed the Magnitude response and Impulse response for LMS and NLMS algorithms which are presented in figure 3 to 6.

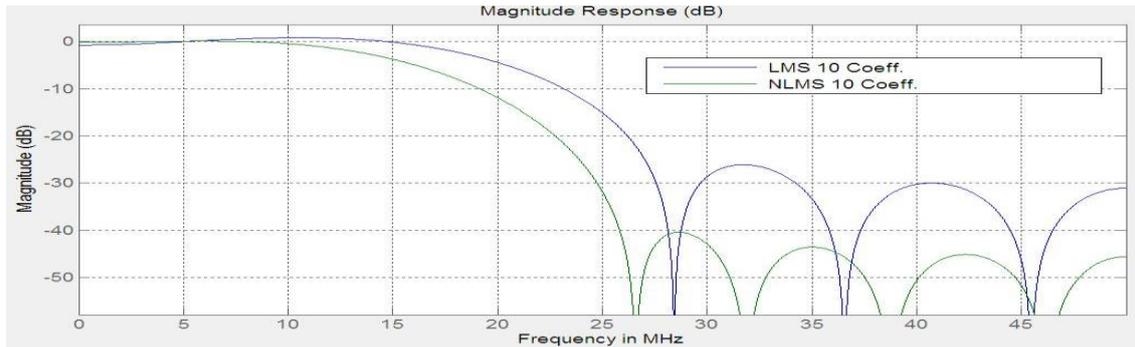


Fig. 3 Magnitude response LMS & NLMS for 10 coefficients.

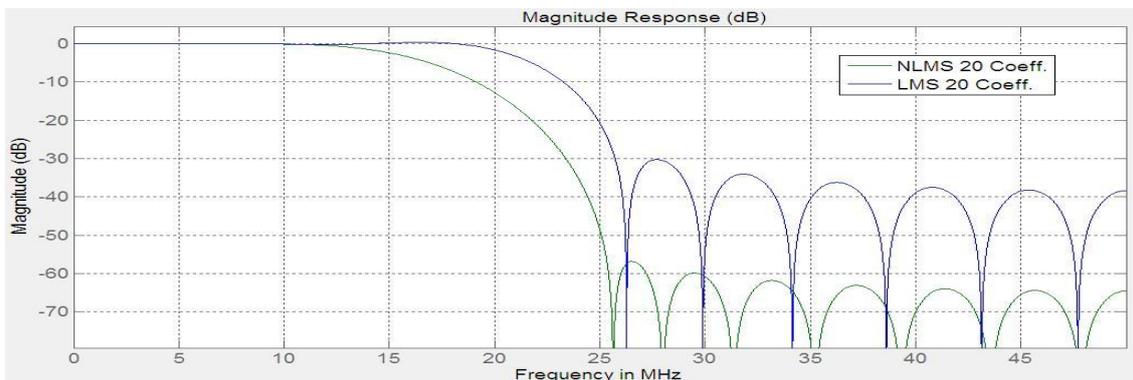


Fig. 4 Magnitude response LMS & NLMS for 20 coefficients.

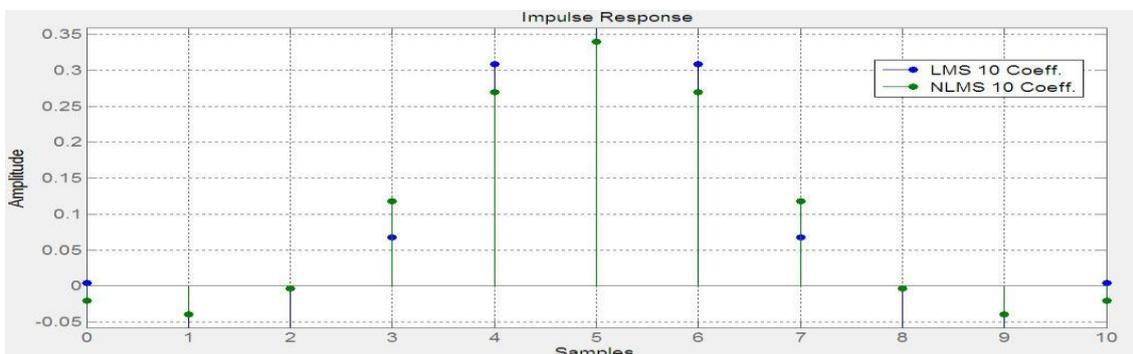


Fig. 5 Impulse response LMS & NLMS for 10 coefficients.

Similarly the Magnitude response and Impulse response for 20 coefficient, LMS and NLMS algorithms are observed.

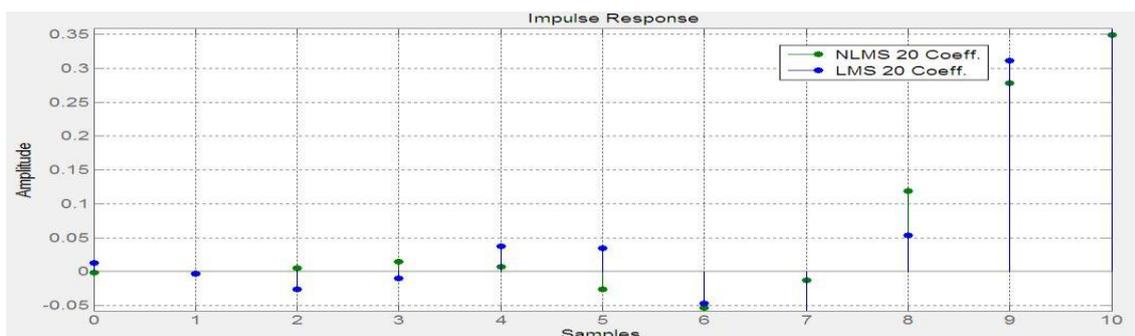


Fig. 6 Impulse response LMS & NLMS for 20 coefficients.

After Matlab simulations the VHDL code of the proposed system is simulated on Xilinx ISE Simulator 12.2 for input and output streams of 16 bit. Figure 7 and 8 presents the simulated wave forms for 10 and 20 coefficients.

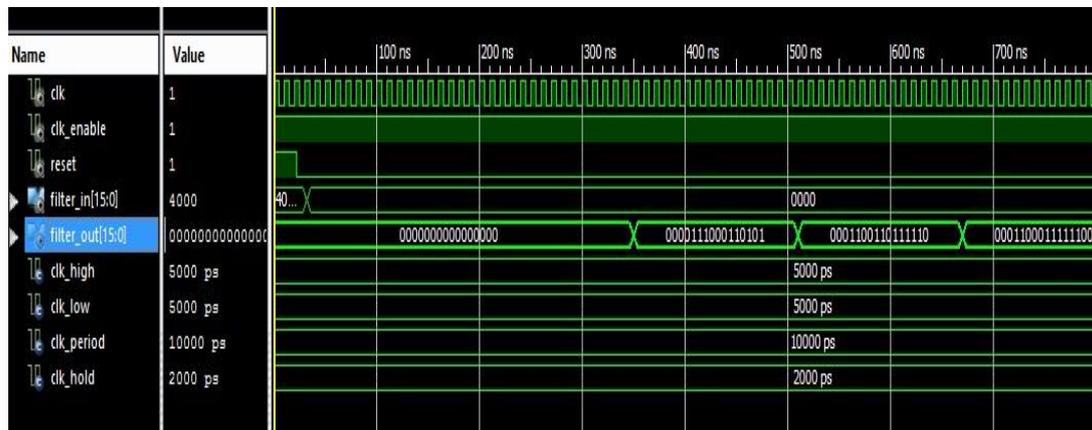


Fig. 7 Simulation waveform NLMS Adaptive filter 10 coefficients.



Fig. 8 Simulation waveform NLMS Adaptive filter 20 coefficients.

The VHDL description of the proposed algorithm is simulated and implemented on a Xilinx Spartan 3 XC 35400 and Spartan 3E FPGA device using DA algorithm by efficiently utilizing LUTs of FPGA target device. We have tabulated details of resource utilized by the design and compared it with one of previous design referred as design [3].

Table 1 Resource Utilization and Speed by using Spartan 3E based Xc3500e FPGA.

Parameter	Utilization for 10 coefficient	Utilization for 20 coefficient	Available
No. of Slices	221	346	4656
No. of slice Flip Flops	165	220	9312
No. of LUTs	413	653	9312
Number of bonded IOBs	35	35	232
Maximum Freq. (MHz)	110.738	127.240	-----
Minimum Period (ns)	9.030	7.859	-----

Table 2 Resource Utilization and Speed by using Spartan 3 based XC 35400 FPGA.

Parameter	Utilization for 10 coefficient	Utilization for 20 coefficient	Available
No. of Slices	222	341	3584
No. of slice Flip Flops	155	212	7168
No. of LUTs	414	642	7168
Number of bonded IOBs	35	35	141
Maximum Freq. (MHz)	107.616	97.207	-----
Minimum Period (ns)	9.292	10.287	-----

On observing table 1 and 2 it is clear that the proposed design is area as well as speed efficient for variable filter orders. Furthermore the performance comparison for the proposed design for adaptive filter is presented in Table 3. We have compared the proposed system with a previous design of adaptive filter presented in design [3]. From table 3 we can observe that the proposed filter of 10 and 20 coefficients can be operated at an estimated frequency 107.616 MHz and 97.207 MHz as compared to 88.89 MHz and 63.04 in existing design [3], with minimum period of 9.292 and 10.287 as compared to existing period of 11.124 and 15.862 respectively by using SPARTAN 3 based XC 35400.

Table 3 Resource comparison for existing and proposed design

Logic utilization & speed	10 coefficients		20 coefficients		Available
	Design [3]	Proposed	Design [3]	Proposed	
No. of Slices	276	222	603	341	3584
No. of Flip Flops	275	155	519	212	7168
No. of LUTs	370	414	854	642	7168
No. of Multipliers	9	0	16	0	-----
Maximum Freq. (MHz)	88.89	107.616	63.04	97.207	-----
Minimum Period (ns)	11.124	9.292	15.862	10.287	-----

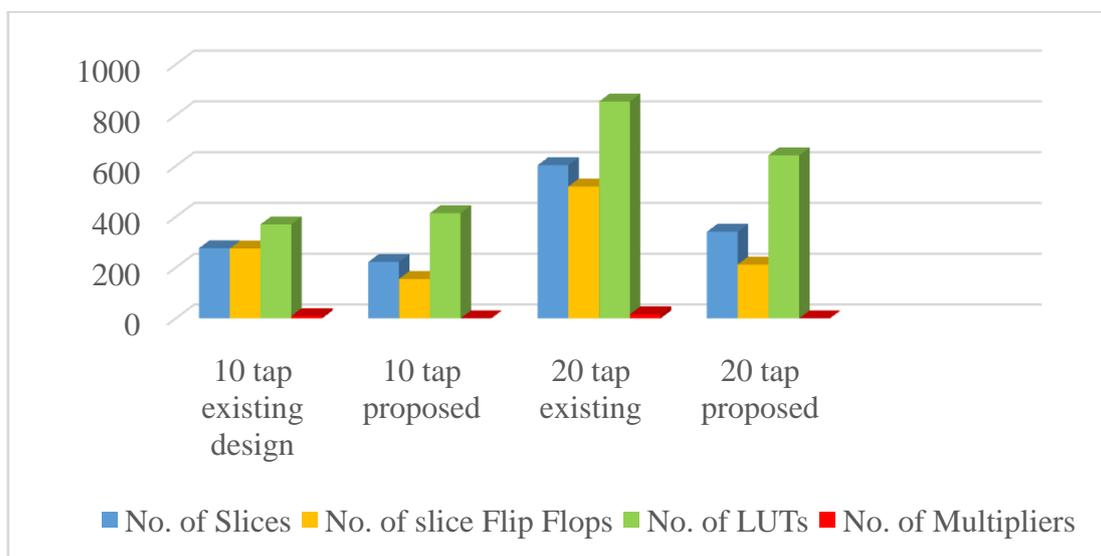


Fig. 9 Comparative Analysis

The developed multiplier less adaptive filter has consumed less number of slices, flip flops and LUTs as compared to existing design. Also in proposed design there is no multiplier used whereas 9 and 16 multipliers are being used by existing design for 10 and 20 coefficient filters respectively.

V. Conclusion

Distributed Arithmetic based Adaptive Filter is implemented with modified NLMS algorithm which uses concept of memory preallocation for variables like input and output signals. We used Matlab for simulation and testing is of the proposed system. Afterwards design is implemented on target FPGA and analysis is done on the basis of number of slices, flip flops, LUTs, IOBs, maximum frequency and minimum period. The proposed filter has been implemented on Spartan 3 based XC 35400 and Spartan 3E based Xc3500e FPGA. Also the comparative analysis has been done with the existing design and it has been observed that DA based proposed design consume less area and provides high speed as compared to existing design. DA based adaptive filter for 10 and 20 coefficient has consumed only 222 and 341 no. of slices, 155 and 212 no. of flip flops, 414 and 642 no. of LUTs respectively. The proposed filter of 10 and 20 coefficients can be operated at an estimated frequency 107.616 MHz and 97.207 MHz, with minimum period of 9.292 and 10.287 respectively by using SPARTAN 3.

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